

Chapter 13 / **Example 7****Average and instantaneous velocity**

A diver jumps from a platform at time $t = 0$ seconds. The distance of the diver above the water level at time t seconds is given by $s(t) = -4.9t^2 + 4.9t + 10$, where s is in metres.

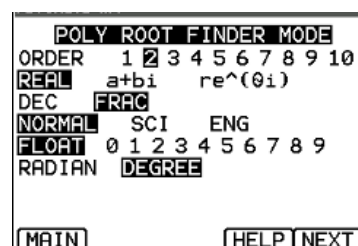
- Find the average velocity of the diver during the dive.
- Find the velocity of the diver at the instant the diver hits the water.
- Explain why the answer to part b is negative.
- Find the speed of the diver at the instant the diver hits the water.

Solve $s(t) = 0$ where $t \geq 0$

Press **[APPS]** :PlySmlt2

Press **[enter]** **[enter]** **[enter]**

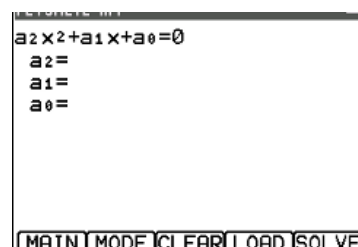
You are solving a quadratic (degree 2) with real roots so press **[f5]** NEXT.



Enter to coefficients into the template. Press **[tab]** to navigate through the template.

$a_2 = -4.9$, $a_1 = 4.9$ and $a_0 = 10$

[f5] SOLVE.



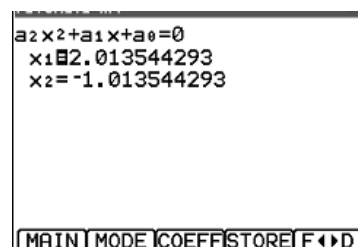
To be able to use the most accurate value of t in the following calculations store this value of t .

Press **[f4]** STORE and choose STORE ROOTS TO LIST.

Press **[enter]** and choose the list L_1 by pressing **[2nd]** **[1]** (**[L1]**).

Press **[enter]**, **[f1]** MAIN and 6:QUIT APP

The positive value x_1 will be stored as $L_1(1)$



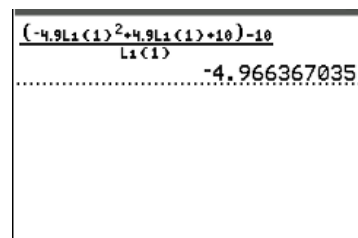
Find the average velocity over the interval $[0, 2.01354]$ using the formula $\frac{s(t) - s(0)}{t - 0}$

Clearly $s(0) = 10$

Press **[ALPHA]** **[f1]** 1:n/d to select the fraction template.

Type $(-4.9 L_1(1) \text{ [x] } + 4.9 L_1(1) + 10) - 10$ in the numerator and $L_1(1)$ in the denominator.

Average velocity = -4.97 ms^{-2} .



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To calculate the instantaneous velocity when diver hits the water find $s'(t)$ when $t = 2.01...$

To calculate the instantaneous rate of change press α [f2] 3:nDeriv

The template has spaces for the variable, x , the function and the value that it is evaluated at.

$$\frac{d}{dt} \left((-4.9L_1(1)^2 + 4.9L_1(1) + 10) - 10 \right) \bigg|_{L_1(1)} = -4.966367035$$

Although the function is expressed in terms of t , the variable used on the GDC will be x .

Enter X in the denominator and type in the function

$-4.9x^2 + 4.9x + 10$. Enter $L_1(1)$ as the value of x .

Press α [enter].

The instantaneous velocity when the diver hits water is -14.8 ms^{-1} .

$$\frac{d}{dx} \left((-4.9L_1(1)^2 + 4.9L_1(1) + 10) - 10 \right) \bigg|_{L_1(1)} = -14.83273407$$