

## Chapter 13 / Example 5

# Modelling Change

Using functions can be an efficient way to make calculations with the GDC.

A company uses the function  $C(x) = 100 + x - 0.01x^2 + 0.00006x^3$  to estimate the cost, in Euros, of producing  $x$  items. The revenue, in Euros, of selling  $x$  items is modelled by  $R(x) = 22.8x - 0.001x^2$ .

- Find the cost of producing 300 items.
- Find the marginal cost of producing 300 items and explain what this means, in context.
- Find the marginal profit of selling 300 items and explain what this means, in context.

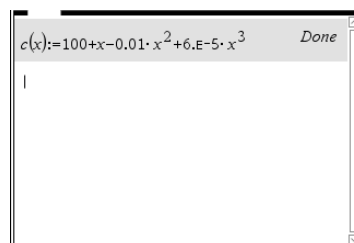
Open a new document and add a Calculator page.

You are first going to define the functions  $C(x)$ ,  $R(x)$  and a profit function  $P(x)$ .

Type  $C(X)$  then press **ctrl** **[=]** (**:=**)

Type  $100 + x - 0.01x^2 + 0.00006x^3$  and press **enter**.

To enter  $^3$ , press **^** **3**

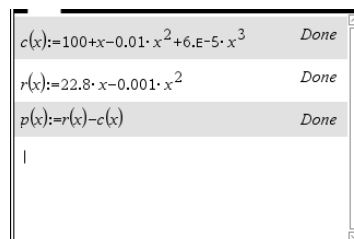


Type  $R(X)$  then press **ctrl** **[=]** (**:=**)

Type  $22.8x - 0.001x^2$  and press **enter**.

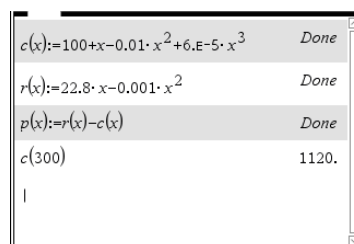
Type  $P(X)$  then press **ctrl** **[=]** (**:=**)

Type  $R(x) - C(x)$  and press **enter**.



Type  $C(300)$  and press **enter**.

The cost of producing 300 items is €1,120



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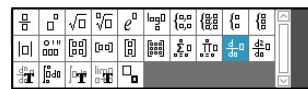
The marginal cost function is the derivative of the cost function. Use a GDC to find  $C'(300)$ .

Press  $\frac{d}{dx}$  and select  $\frac{d}{dx}$

Enter X in the denominator and the function C ( X )

Enter  $\text{ctrl} = ( \neq )$  and select the vertical bar ( | )

Type X = 300 and press  $\text{enter}$ .



The marginal cost of producing 300 items,  $C'(300)$ , is €11.20

$r(x) := 100 + x - 0.01 \cdot x^2 + 6 \cdot E^{-5} \cdot x^3$	Done
$r(x) := 22.8 \cdot x - 0.001 \cdot x^2$	Done
$p(x) := r(x) - c(x)$	Done
$c(300)$	1120.
$\frac{d}{dx}(c(x)) _{x=300}$	11.2

The marginal profit function is the derivative of the profit function. Use a GDC to find  $P'(300)$ .

Press  $\frac{d}{dx}$  and select  $\frac{d}{dx}$

Enter X in the denominator and the function P ( X )

Enter  $\text{ctrl} = ( \neq )$  and select the vertical bar ( | )

Type X = 300 and press  $\text{enter}$ .



The marginal cost of selling 300 items,  $P'(300)$ , is €11.

$p(x) := r(x) - c(x)$	Done
$c(300)$	1120.
$\frac{d}{dx}(c(x)) _{x=300}$	11.2
$\frac{d}{dx}(p(x)) _{x=300}$	11.