

Using a graphic display calculator

CHAPTER OBJECTIVES:

This chapter shows you how to use your graphic display calculator (GDC) to solve the different types of problems that you will meet in your course. You should not work through the whole of the chapter – it is simply here for reference purposes. When you are working on problems in the mathematical chapters, you can refer to this chapter for extra help with your GDC if you need it.

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






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Before you start

You should know:

- Important keys on the keyboard: , , , , , , , , 
- The home screen
- Opening new documents, adding new pages, changing settings
- Moving between pages in a document
- Panning and grabbing axes to change a window in a Graphs page
- Change window settings in a Graphs page
- Using zoom tools in a Graphs page
- Using trace in a Graphs page
- Setting the number of significant figures or decimal places

1 Functions

1.1 Graphing linear functions

Example 1


Draw the graph of the function $y = 2x + 1$

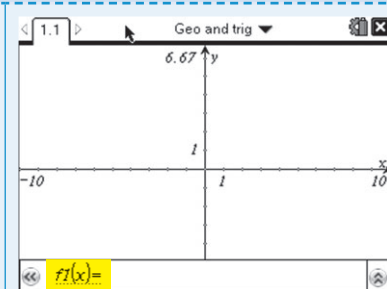
Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area.

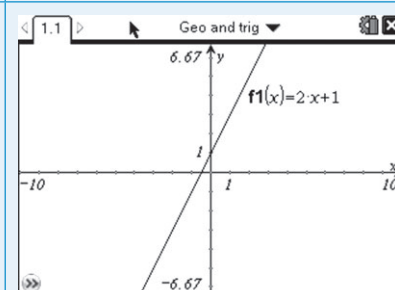
The default graph type is Function,
so the form ' $f1(x)=$ ' is displayed.

The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.

Type $2x + 1$ and press .



The graph of $y = 2x + 1$ is now displayed and labeled on the screen.



Finding information about the graph

Your GDC can give you a lot of information about the graph of a function, such as the coordinates of points of interest and the gradient (slope).

1.2 Finding a zero

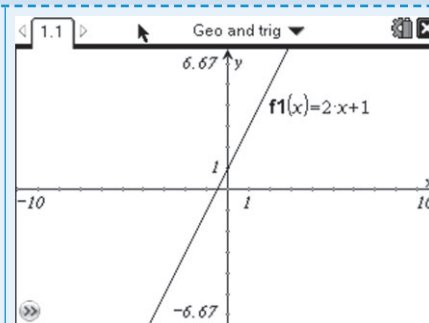
The x -intercept is known as a *zero* of the function.

At the x -intercept, $y = 0$.

Example 2

Find the zero of $y = 2x + 1$

First draw the graph of $y = 2x + 1$ (see Example 1).



Press **menu** 6:Analyze Graph | 1:Zero

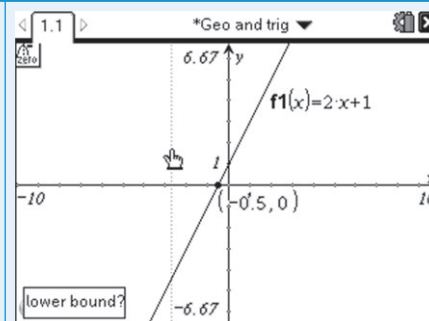
Press **enter**

To find the zero you need to give the lower and upper bounds of a region that includes the zero.

The GDC shows a line and asks you to set the lower bound.

Move the line using the touchpad and choose a position to the left of the zero.

Click the touchpad.

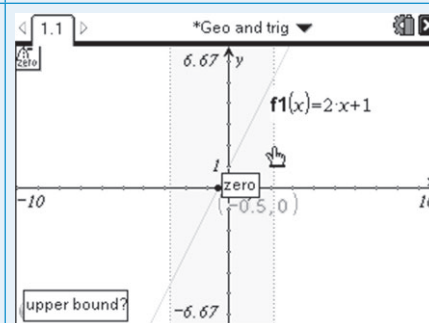


The GDC shows another line and asks you to set the upper bound.

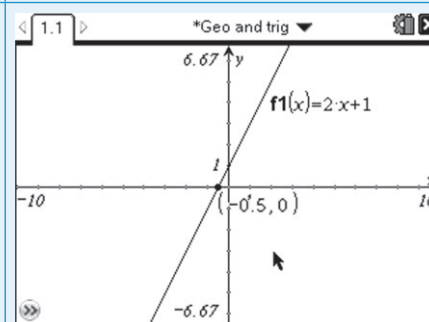
Use the touchpad to move the line so that the region between the upper and lower bounds contains the zero.

When the region contains the zero, the calculator will display the word 'zero' in a box.

Click the touchpad.



The GDC displays the zero of the function $y = 2x + 1$ at the point $(-0.5, 0)$.



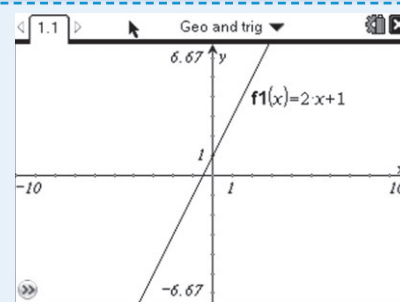
1.3 Finding the gradient (slope) of a line

The correct mathematical notation for gradient (slope) is $\frac{dy}{dx}$, and this is how the GDC denotes gradient.

Example 3

Find the gradient of $y = 2x + 1$

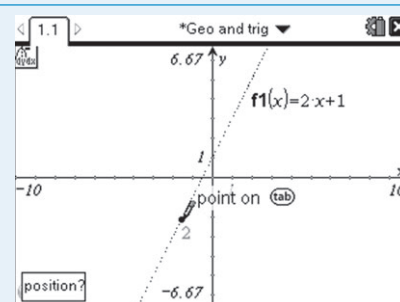
First draw the graph of $y = 2x + 1$ (see Example 1).



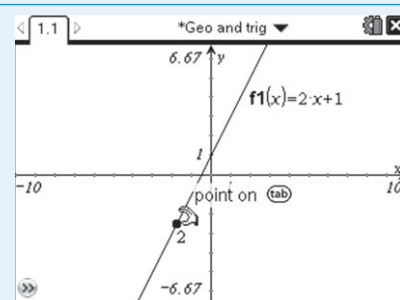
Press **menu** 6:Analyse Graph | 5: $\frac{dy}{dx}$

Press **enter**

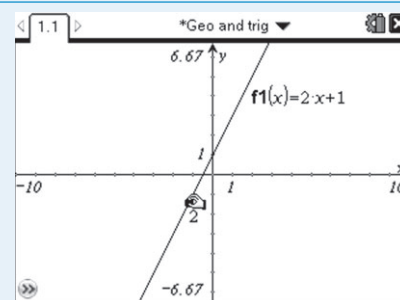
Use the touchpad to select a point on the line.
Click the touchpad.



The point you selected is now displayed together with the gradient of the line at that point.
The gradient (slope) is 2.



With the open-hand symbol showing, click the touchpad again. The hand is now grasping the point.
Move the point along the line using the touchpad.
This confirms that the gradient (slope) of $y = 2x + 1$ at every point on the line is 2.



1.4 Solving simultaneous equations graphically

To solve simultaneous equations graphically you draw the straight lines and then find their point of intersection. The coordinates of the point of intersection give you the solutions x and y .

Example 4

Use a graphical method to solve the simultaneous equations

$$\begin{aligned} 2x + y &= 10 \\ x - y &= 2 \end{aligned}$$

For solving simultaneous equations using a non-graphical method, see section 1.5.

► Continued on next page

First rewrite both equations in the form ' $y =$ '.

$$2x + y = 10$$

$$y = 10 - 2x$$

$$x - y = 2$$

$$-y = 2 - x$$

$$y = x - 2$$

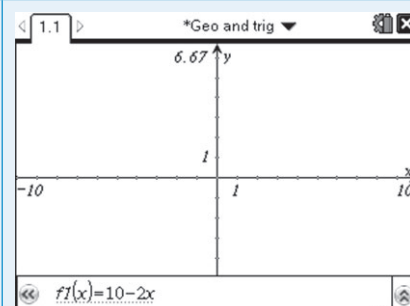
The GDC will only draw the graphs of functions that are expressed explicitly, ' $y =$ ' as a function of x . If the equations are written in a different form, you need to rearrange them before using your GDC to solve them.

To draw the graphs $y = 10 - 2x$ and $y = x - 2$:

Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x)=$ ' is displayed.

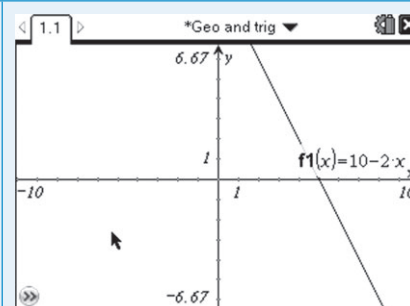
The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



Type $10 - 2x$ and press **enter**.

The calculator displays the first straight-line graph:

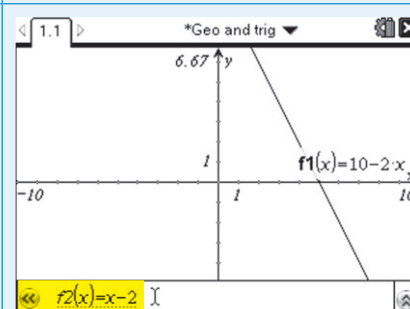
$$f1(x) = 10 - 2x$$



Use the touchpad to click on the arrows in the bottom left-hand corner of the screen.

This will open the entry line again. This time ' $f2(x)=$ ' is displayed.

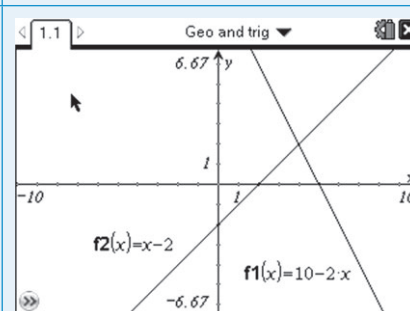
Type $x - 2$ and press **enter**.



The GDC now displays both straight-line graphs:

$$f1(x) = 10 - 2x$$

$$f2(x) = x - 2$$



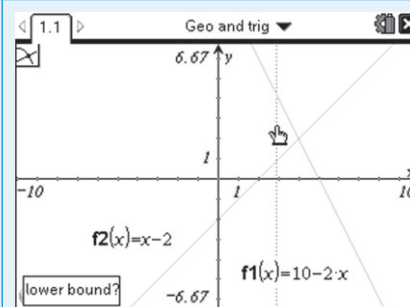
Press **menu** 6:Analyze Graph | 4:Intersection Point(s)

Press **enter**

To find the intersection you need to give the lower and upper bounds of a region that includes the intersection.

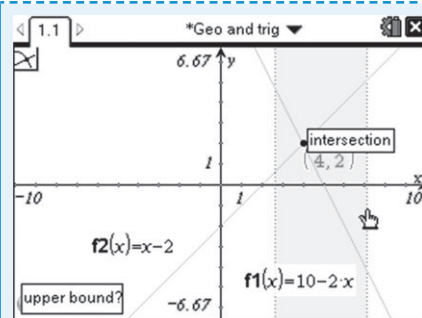
The GDC shows a line and asks you to set the lower bound. Move the line using the touchpad and choose a position to the left of the intersection.

Click the touchpad.

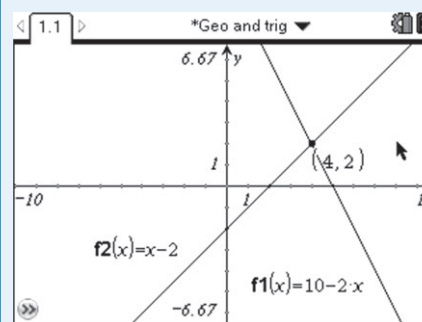


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The GDC shows another line and asks you to set the upper bound. Use the touchpad to move the line so that the region between the upper and lower bounds contains the intersection. When the region contains the intersection, the calculator will display the word 'intersection' in a box. Click the touchpad.



The calculator displays the intersection of the two straight lines at the point (4, 2). The solution is $x = 4$, $y = 2$.



Simultaneous and quadratic equations

1.5 Solving simultaneous linear equations in two unknowns

When solving simultaneous equations in an examination, you do not need to show any method of solution. You should simply write out the equations in the correct form and then give the solutions. The GDC will do all the working for you.

You do not need the equations to be written in any particular format to use the linear equation solver, as long as they are both *linear*, that is, neither equation contains x^2 or higher order terms.

Example 5

Solve the equations: $2x + y = 10$
 $x - y = 2$

Open a new document and add a Calculator page.
Press **menu** 3:Algebra | 2:Solve Systems of Linear Equations...
Press **enter**
You will see this dialogue box, showing 2 equations and two variables, x and y .

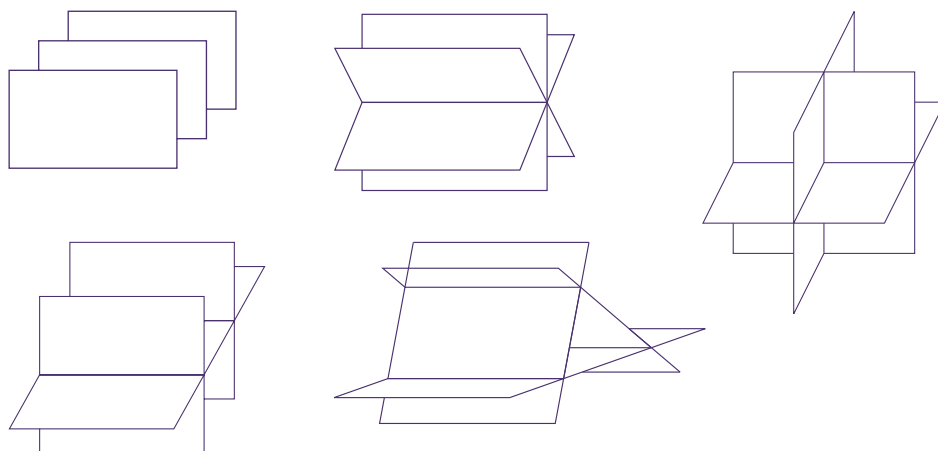
Note: This is how you will use the linear equation solver in your examinations. In your project you might solve a more complicated system (more equations and more variables).

Press **enter** and you will see the template on the right.
Type the two equations into the template, using the arrow keys \blacktriangle \blacktriangledown to move within the template.
Press **enter** and the GDC will solve the equations, giving the solutions in the form $\{x, y\}$.

The solutions are $x = 4$, $y = 2$.

1.6 Solving simultaneous equations in three unknowns

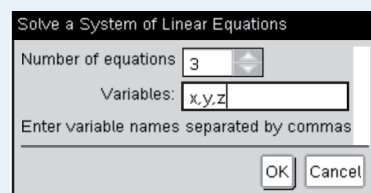
When solving simultaneous equations in three unknowns there might be a unique solution, infinitely many solutions or no solutions at all. Geometrically, if the equations represent planes in three-dimensions, then their solutions would be intersection at a point, intersection on a line (or plane) or non-intersecting planes.



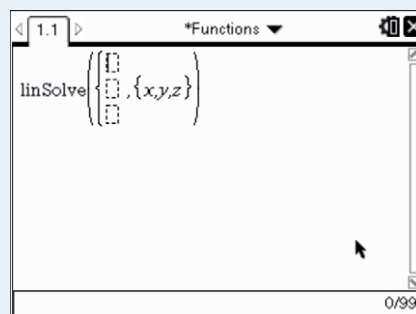
Example 6

Solve the equations $2x - 3y + 4z = 1$
 $x - y - z = -1$
 $-x + 2y - z = 2$

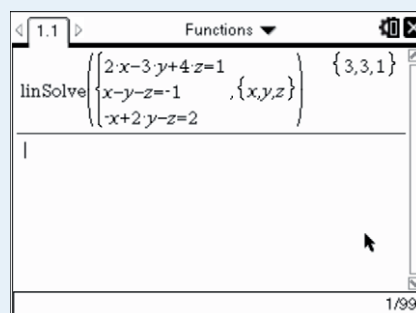
Open a new document and add a Calculator page.
 Press menu 3:Algebra | 2:Solve Systems of Linear Equations...
 Press **enter**
 Edit the dialog box to show three equations and three variables, x , y and z .



Press **enter** and you will see the template on the right.
 Type the two equations into the template, using the arrow keys \blacktriangle \blacktriangledown to move within the template.
 Press enter and the GDC will solve the equations, giving the solutions in the form $\{x, y, z\}$.



The solutions are $x = 3$, $y = 3$ and $z = 1$
 In this example, the solutions represent a point.

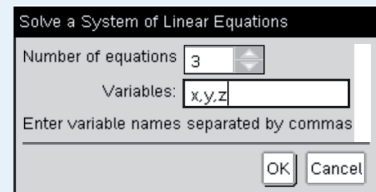


Example 7

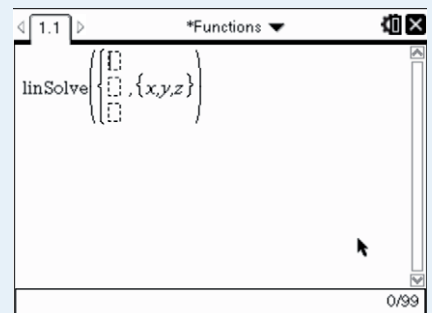
Solve the equations

$$\begin{aligned} 2x + 4y + 2z &= 8 \\ x + 2y + z &= 4 \\ 3x - y + z &= -9 \end{aligned}$$

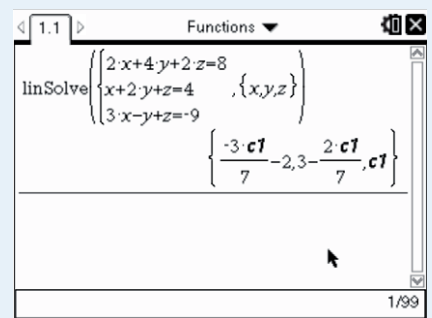
Open a new document and add a Calculator page.
Press menu 3:Algebra | 2:Solve Systems of Linear Equations...
Press **enter**
Edit the dialog box to show three equations and three variables, x , y and z .



Press **enter** and you will see the template on the right.
Type the two equations into the template, using the arrow keys \blacktriangle \blacktriangledown to move within the template.
Press enter and the GDC will solve the equations, giving the solutions in the form $\{x, y, z\}$.



The solutions are $x = \frac{-3c1}{7} - 2$, $y = 3 - \frac{2c1}{7}$ and $z = c1$
In this example, the solutions represent a straight line.
Since $z = c1$ (an arbitrary constant), the equations of the line can be written
$$\frac{7(x+2)}{-3} = \frac{7(y-3)}{-2} = z$$
$$\frac{x+2}{3} = \frac{y-3}{2} = \frac{z}{-7}$$

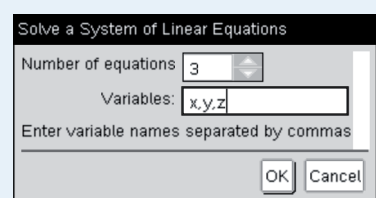


Example 8

Solve the equations

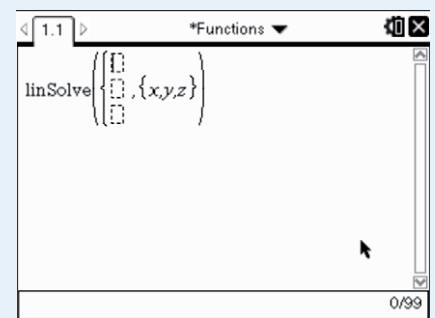
$$\begin{aligned} x + 2y - 3z &= 13 \\ 2x - y + x &= 4 \\ x + 2y - 3z &= 7 \end{aligned}$$

Open a new document and add a Calculator page.
Press menu 3:Algebra | 2:Solve Systems of Linear Equations...
Press **enter**
Edit the dialog box to show three equations and three variables, x , y and z .



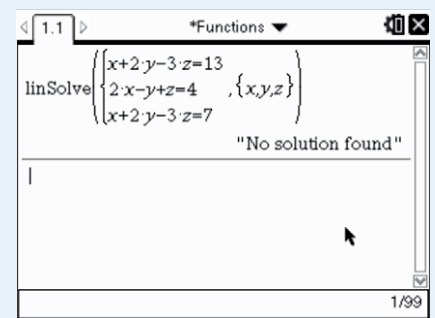
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Press **enter** and you will see the template on the right.
 Type the two equations into the template, using the arrow keys \blacktriangle \blacktriangledown to move within the template.
 Press enter and the GDC will solve the equations, giving the solutions in the form $\{x, y, z\}$.



There are no solutions.

In this example the equations are inconsistent.



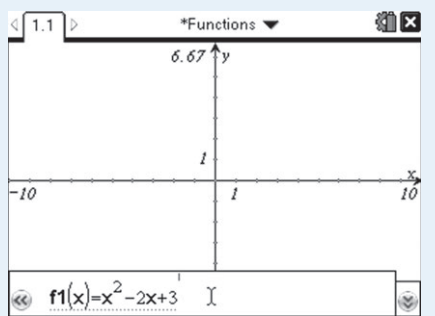
Quadratic functions

1.7 Drawing a quadratic graph

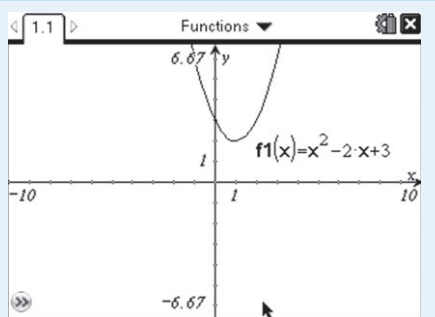
Example 9

Draw the graph of $y = x^2 - 2x + 3$ and display using suitable axes.

Open a new document and add a Graphs page.
 The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x) =$ ' is displayed.
 The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.

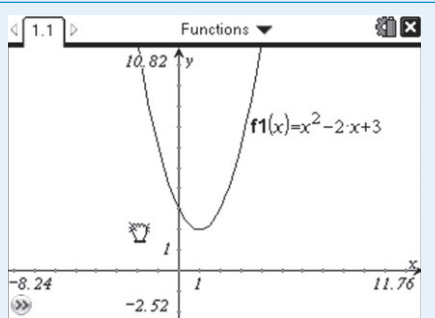


Type $x^2 - 2x + 3$ and press **enter**.
 The calculator displays the curve with the default axes.



Pan the axes to get a better view of the curve.

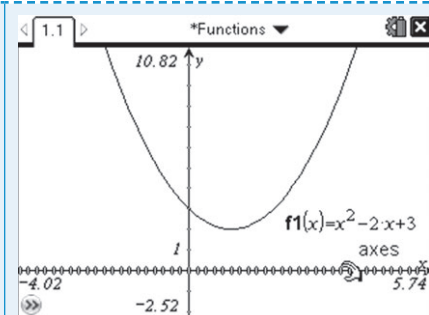
For help with panning,
 see your GDC manual.



► Continued on next page

Grab the x -axis and change it to make the quadratic curve fit the screen better.

For help with changing axes, see your GDC manual.



1.8 Solving quadratic equations

When solving quadratic equations in an examination, you do not need to show any method of solution. You should simply write out the equations in the correct form and then give the solutions. The GDC will do all the working for you.

Example 10

Solve $3x^2 - 4x - 2 = 0$

Press **menu** 3:Algebra | 3:Polynomial Tools | 1:Find Roots of a Polynomial...

Press **enter**

You will see this dialogue box, showing a polynomial of degree 2 (a quadratic equation) with real roots. You do not need to change anything.

Press **enter**

Another dialogue box opens for you to enter the equation.

The general form of the quadratic equation is

$a_2x^2 + a_1x + a_0 = 0$, so enter the coefficients in

a_2 , a_1 and a_0 .

Here, $a_2 = 3$, $a_1 = -4$ and $a_0 = -2$. Be sure to use the **(-)** key to enter the negative values. Use the **tab** key to move around the dialogue box.

Press **enter** and the GDC will solve the equation, giving the roots in the form $\{x, y\}$.

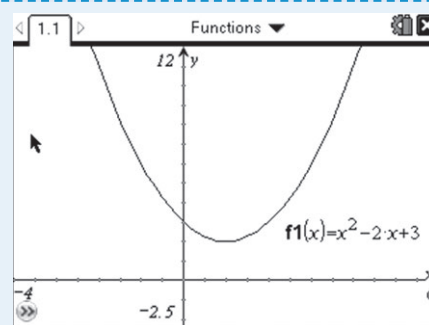
The solutions are $x = -0.387$ or $x = 1.72$ (to 3 sf).

1.9 Finding a local minimum or maximum point

Example 11

Find the minimum point on the graph of $y = x^2 - 2x + 3$

First draw the graph of $y = x^2 - 2x + 3$ (see Example 6).



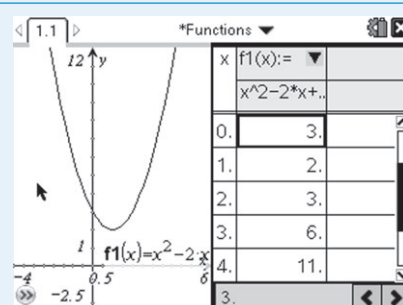
Method 1: Using a table

You can look at the graph **and** a table of the values by using a split screen.

Press **menu** 2:View | 9:Show Table

(or simply press **ctrl** **T**)

The minimum value shown in the table is 2 when $x = 1$.



Look more closely at the values of the function around $x = 1$.

Change the settings in the table.

Choose any cell and press **menu** 5:Table | 5:Edit Table Settings...

Set Table Start to 0.98 and Table Step to 0.01.

Press **enter**

Table

Table Start:

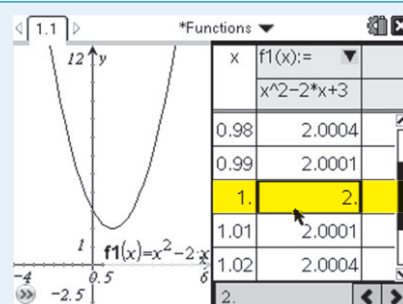
Table Step:

Independent:

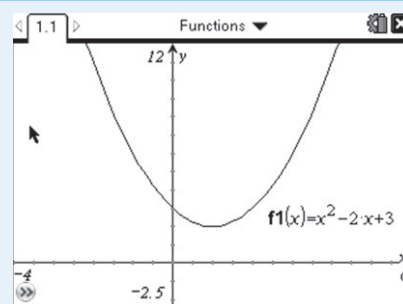
Dependent:

OK **Cancel**

The table shows that the function has larger values at points around (1, 2). We can conclude that the point (1, 2) is a local minimum on the curve.



Method 2: Using the minimum function



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Press **menu** 6:Analyze Graph | 2:Minimum

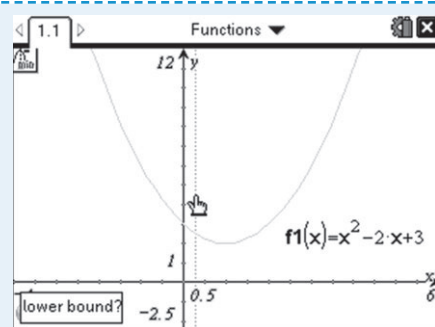
Press **enter**

To find the minimum you need to give the lower and upper bounds of a region that includes the minimum.

The GDC shows a line and asks you to set the lower bound.

Move the line using the touchpad and choose a position to the left of the minimum.

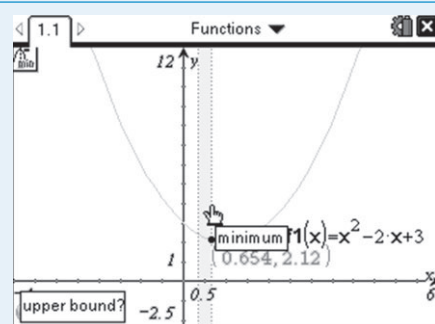
Click the touchpad.



The GDC shows another line and asks you to set the upper bound.

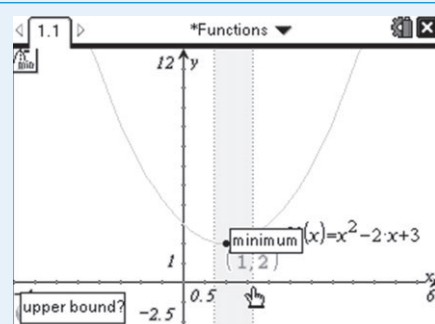
Use the touchpad to move the line so that the region between the upper and lower bounds contains the minimum.

Note: The minimum point in the region that you have defined is being shown. In this screenshot it is not the local minimum point. Make sure you move the line beyond the point you are looking for.

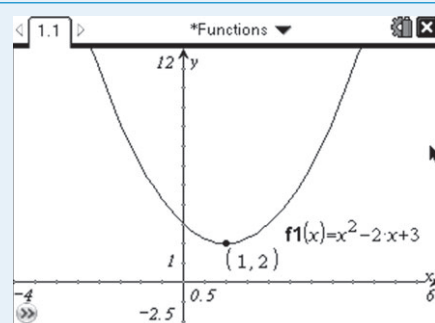


When the region contains the minimum, the GDC will display the word 'minimum' in a box and a point that lies between the lower and upper bounds. The point displayed is clearly between the upper and lower bounds.

Click the touchpad.



The calculator displays the minimum point on the curve at (1, 2).



Example 12

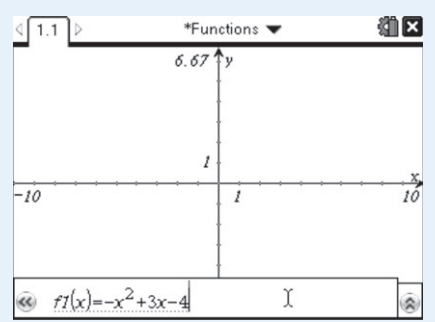
Find the maximum point on the graph of $y = -x^2 + 3x - 4$

First draw the graph of $y = -x^2 + 3x - 4$:

Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x)=$ ' is displayed.

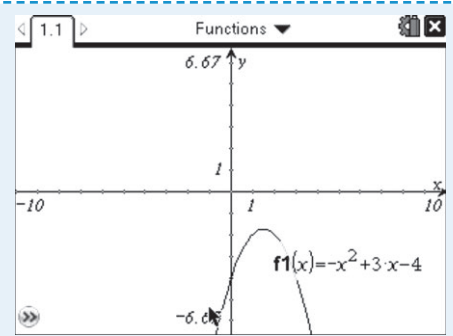
The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



▶ Continued on next page

Type $-x^2 + 3x - 4$ and press **enter**.

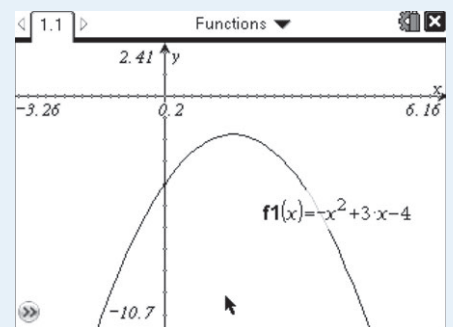
The GDC displays the curve with the default axes.



Pan the axes to get a better view of the curve.

Grab the x -axis and change it to make the quadratic curve fit the screen better.

For help with panning or changing axes, see your GDC manual.



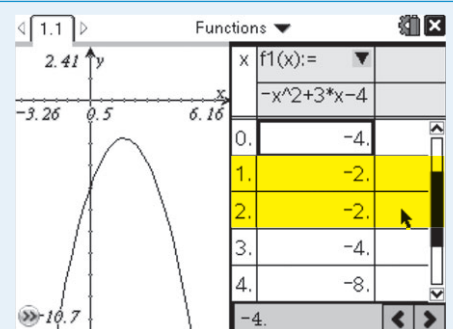
Method 1: Using a table

You can look at the graph **and** a table of the values by using a split screen.

Press **menu** 2:View | 9:Show Table

(or simply press **ctrl** **T**)

The maximum value shown in the table is -2 when $x = 1$ and $x = 2$.



Look more closely at the values of the function between $x = 1$ and $x = 2$.

Change the settings in the table.

Choose any cell and press **menu** 5:Table | 5:Edit Table Settings...

Set Table Start to 1.0 and Table Step to 0.1.

Press **enter**

Table

Table Start:

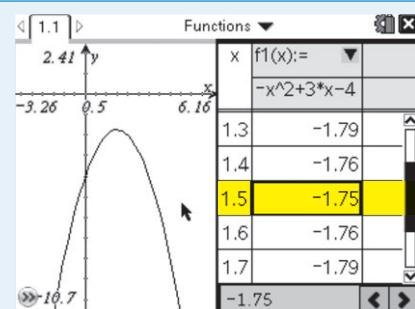
Table Step:

Independent:

Dependent:

OK **Cancel**

Scroll down the table and you can see that the function has its largest value at $(1.5, -1.75)$. We can conclude that the point $(1.5, -1.75)$ is a local maximum on the curve.



► Continued on next page

Method 2: Using the maximum function

Press **menu** 6:Analyze Graph | 3:Maximum

Press **enter**

To find the maximum you need to give the lower and upper bounds of a region that includes the maximum.

The GDC shows a line and asks you to set the lower bound.

Move the line using the touchpad and choose a position to the left of the maximum.

Click the touchpad.

The GDC shows another line and asks you to set the upper bound.

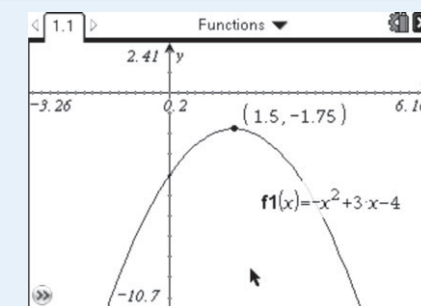
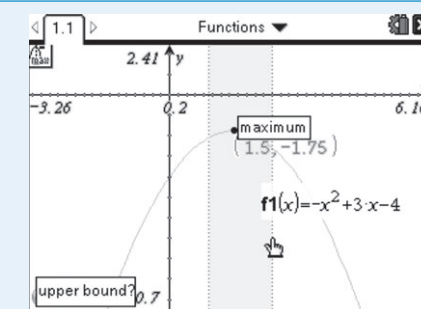
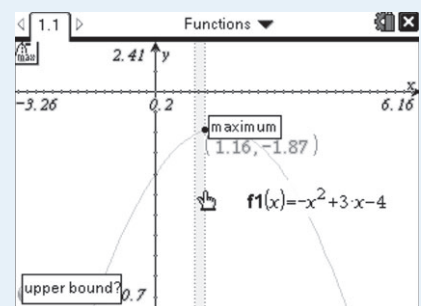
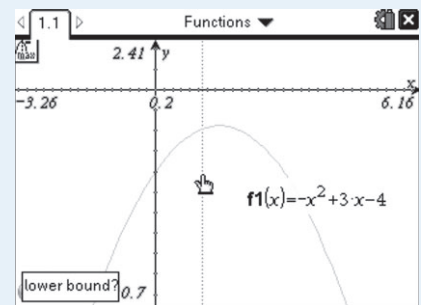
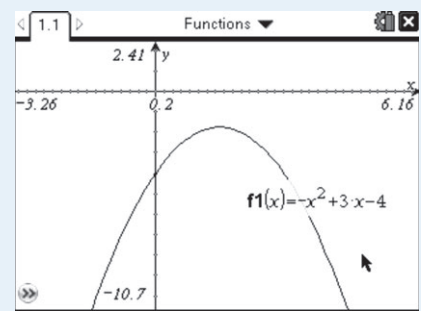
Use the touchpad to move the line so that the region between the upper and lower bounds contains the maximum.

Note: The maximum point in the region that you have defined is being shown. In this screenshot it is not the local maximum point. Make sure you move the line beyond the point you are looking for.

When the region contains the maximum, the GDC will display the word 'maximum' in a box and a point that lies between the lower and upper bounds. The point displayed is clearly between the upper and lower bounds.

Click the touchpad.

The GDC displays the maximum point on the curve at (1.5, -1.75).



Complex numbers

1.10 Operations with complex numbers

Example 13

Evaluate the following expressions

- i $2(7+i) + \frac{1}{2}(4-2i)$ ii $(2+3i) \cdot (3-4i)$
 iii $\sqrt{3+4i}$ iv $\frac{1-i}{3+i}$
 v $(1-i)^3$

Open a new document and add a Calculator page.

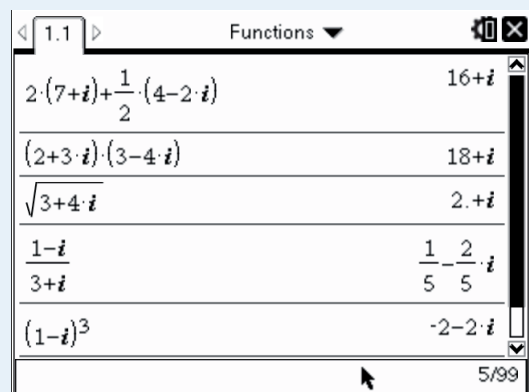
Complex calculations are entered the same way as you would enter a real expression.

To enter imaginary number symbol i press the π key and select i .



Enter the expressions and then press **enter**.

The results are as shown.



1.11 Conjugate, modulus and argument

Example 14

Let $z = 1 + \sqrt{3}i$

Find i z^*

ii $|z|$

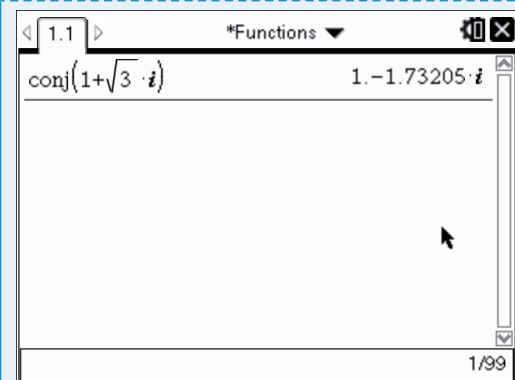
iii $\arg(z)$

Open a new document and add a Calculator page.

- i Press **menu** | 2: Number | 9: Complex Number Tools | 1: Complex Conjugate

Enter the complex number. To enter the imaginary number symbol i press the π key and select i .

Press **enter**.

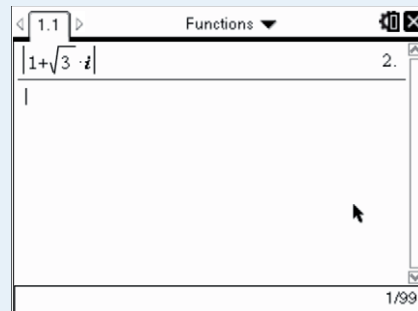


▶ Continued on next page

- ii Press **menu** | 2: Number | 9: Complex Number Tools | 5: Magnitude

Enter the complex number. To enter the imaginary number symbol i press the **π** key and select i .

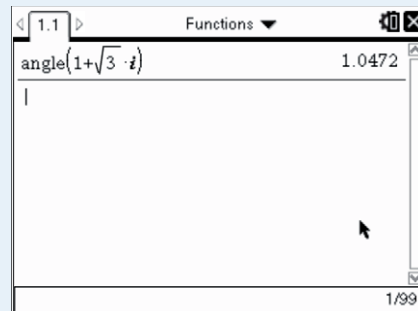
Press **enter**.



- iii Press **menu** | 2: Number | 9: Complex Number Tools | 4: Polar Angle

Enter the complex number. To enter the imaginary number symbol i press the **π** key and select i .

Press **enter**.



1.12 Solving equations with complex roots

Example 15

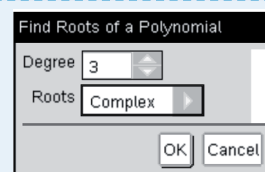
Solve the equation $2x^3 - 15x^2 + 44x - 39 = 0$

Open a new document and add a Calculator page.

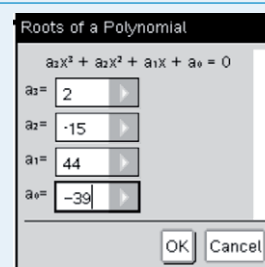
Press **menu** 3: Algebra | 3: Polynomial Tools | 1: Find Roots of Polynomial ...

Select Degree 3 and Complex Roots.

Click OK



Enter the coefficients of the cubic polynomial in a_3 , a_2 , a_1 and a_0
Click OK

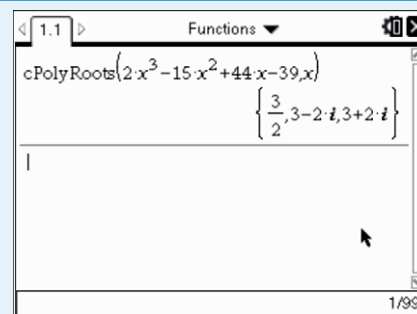


Press **enter**.

Alternatively press **menu** 3: Algebra | 3: Polynomial Tools | 3:Complex Roots of Polynomial and enter the equation directly in the format shown.

The solutions are,

$x = 1.5$, $x = 3 - 2i$ and $x = 3 + 2i$.



1.13 Polar form

The GDC displays complex numbers in either Cartesian form ($z = x + yi$) or in Euler's form ($z = re^{i\theta}$), but not in modulus, argument form – see 1.11 for how to find the modulus and argument of a complex number expressed in Cartesian form.

Example 16

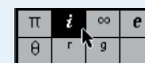
i Change $2 + 2i$ to polar form

ii Change $3e^{\frac{2\pi}{3}i}$ to Cartesian form.

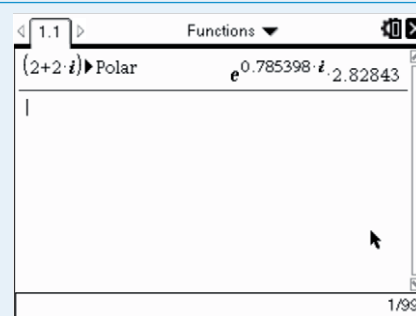
Open a new document and add a Calculator page.

Complex calculations are entered the same way as you would enter a real expression.

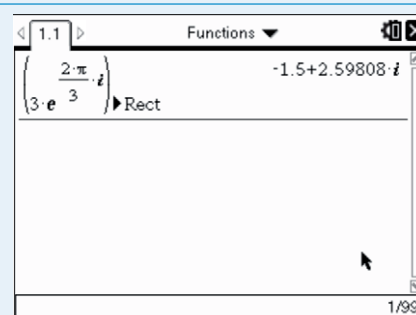
To enter imaginary number symbol i press the π key and select i .




i Enter $2 + 2i$ and then press menu | 2:Number | 9:Complex Number Tools | 6:Convert to Polar
Press enter .



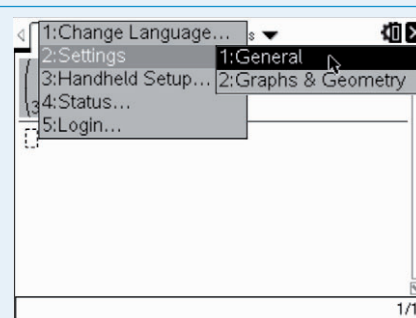
ii Enter $3e^{\frac{2\pi}{3}i}$ and then press menu | 2:Number | 9:Complex Number Tools | 7:Convert to Rectangular
Press enter .



You can also change the mode that the calculator uses to display complex results in settings.

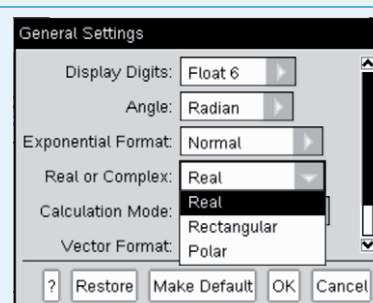
Click on the  icon in the corner of the screen.

Select 2:Settings | 1:General



In the Real or Complex dropdown box select Real, Rectangular or Polar.

For example, in Polar mode, typing $2 + 2i$ enter would result in the number being displayed in polar form without entering \blacktriangleright Polar.



Exponential functions

1.14 Drawing an exponential graph

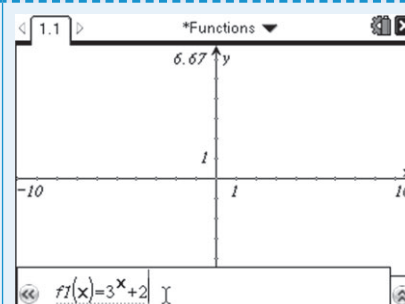
Example 17

Draw the graph of $y = 3^x + 2$

Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x) =$ ' is displayed.

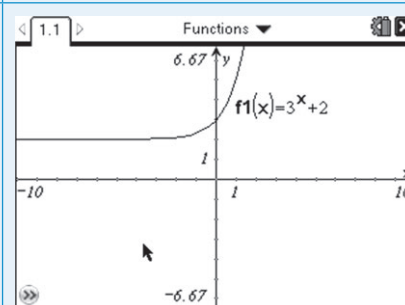
The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



Type $y = 3^x + 2$ and press **enter**.

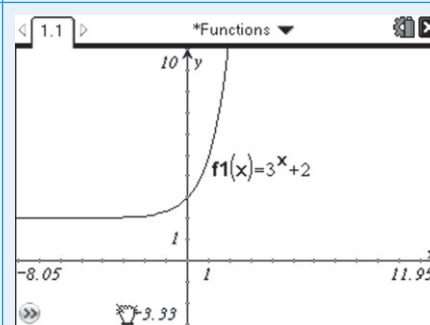
(**Note:** Type **3** **^** **x** **▶** to enter 3^x . The **▶** returns you to the baseline from the exponent.)

The GDC displays the curve with the default axes.



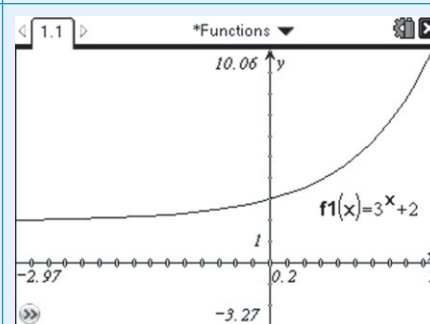
Pan the axes to get a better view of the curve.

For help with panning,
see your GDC manual.



Grab the x -axis and change it to make the exponential curve fit the screen better.

For help with changing
axes, see your GDC
manual.

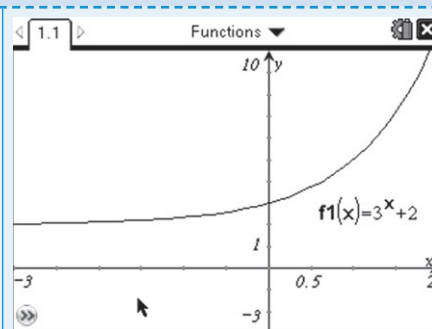


1.15 Finding a horizontal asymptote

Example 18

Find the horizontal asymptote to the graph of $y = 3^x + 2$

First draw the graph of $y = 3^x + 2$ (see Example 17).

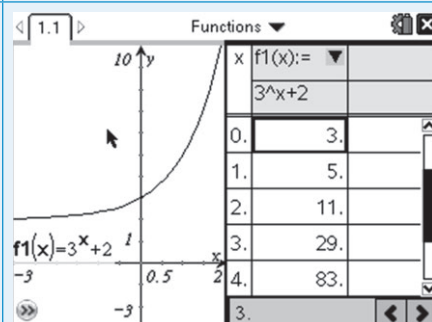


You can look at the graph **and** a table of the values by using a split screen.

Press **menu** 2:View | 9:Show Table

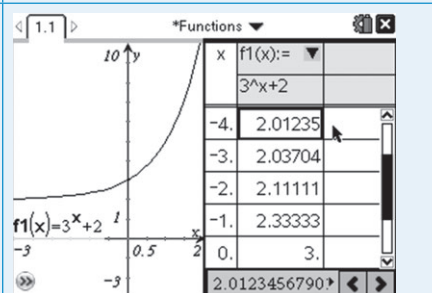
(or simply press **ctrl** **T**)

The values of the function are clearly decreasing as $x \rightarrow 0$.



Press and hold **▲** to scroll up the table.

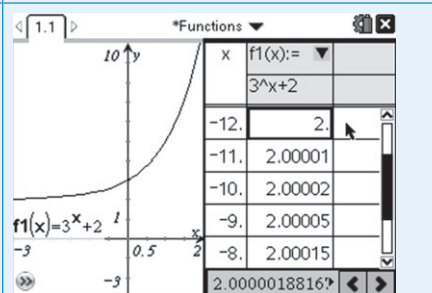
The table shows that as the values of x get smaller, $f1(x)$ approaches 2.



Eventually, the value of $f1(x)$ reaches 2. On closer inspection, you can see, at the bottom of the screen, that the actual value of $f1(x)$ is 2.0000018816...

We can say that $f1(x) \rightarrow 2$ as $x \rightarrow -\infty$.

The line $y = 2$ is a horizontal asymptote to the curve $y = 3^x + 2$.



Logarithmic functions

1.16 Evaluating logarithms

Example 19

Evaluate $\log_{10} 3.95$, $\ln 10.2$ and $\log_5 2$.

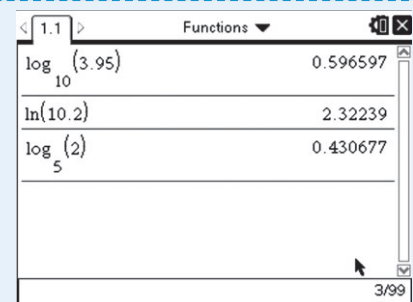
Open a new document and add a Calculator page.

Press **ctrl** **log** to open the log template.

Enter the base and the argument then press **enter** **del**

For natural logarithms it is possible to use the same method, with the base equal to e , but it is far less time consuming to press **ctrl** **ln**.

Note that the GDC will evaluate logarithms with any base without having to use the change of base formula.



1.17 Finding an inverse function

The inverse of a function can be found by interchanging the x and y values. Geometrically this can be done by reflecting points in the line $y = x$.

Example 20

Show that the inverse of the function $y = 10^x$ is $y = \log_{10} x$ by reflecting $y = 10^x$ in the line $y = x$.

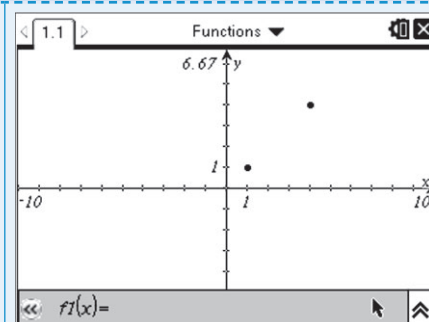
Open a new document and add a Graphs page.

First we will draw the line $y = x$. So that it can be recognised the axis of reflection, it has to be drawn and not plotted as a function.

Press **menu** 7: Points & Lines | 1: Point

Then type **(1 enter 1 enter** then **(4 enter 4 enter esc**

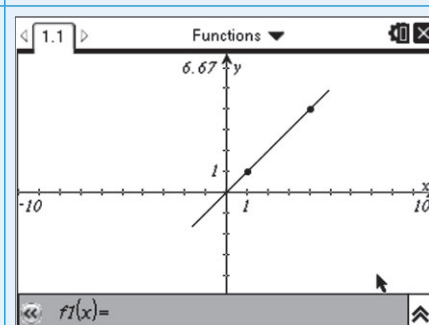
This will plot the points (1, 1) and (4, 4), which both lie on the line $y = x$



Press **menu** 7: Points & Lines | 4: Line

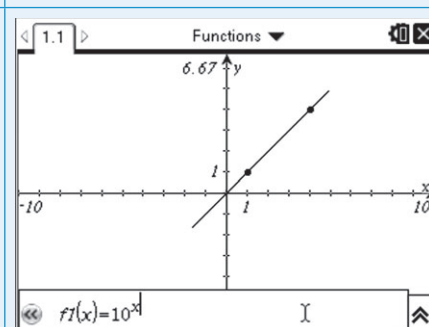
Select both the points you have plotted and draw a line through them.

Press **esc** to exit the drawing function.

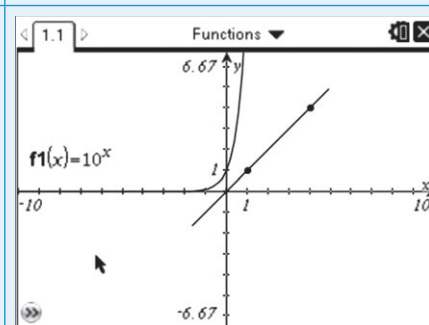


Click in the entry line at the bottom of the work area. The default graph type is Function, so the form " $f1(x) =$ " is displayed.

Type 10^x and press **enter**.



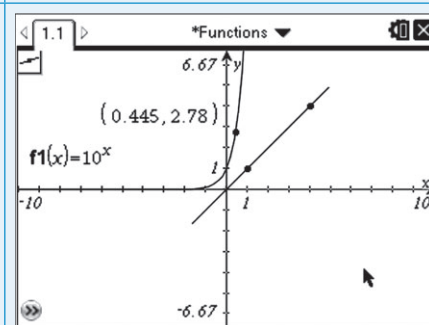
The calculator displays the function with the default axes, $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



Press **menu** 7: Points & Lines | 2: Point On

Select the curve with the touchpad (you will see that it is highlighted when it is selected).

You can place a point anywhere on the curve.

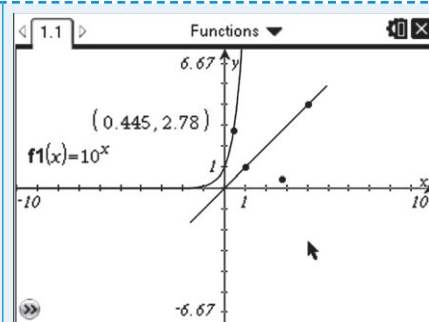


Continued on next page

Press **menu** B: Transformation | 2: Reflection

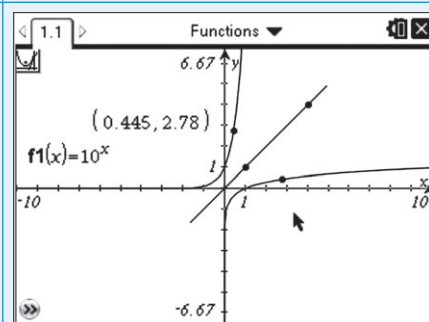
Use the touch pad to select the point that you just placed on the curve and then the line $y = x$.

Press **esc** when you have finished. You should see the reflected image of the point in the line $y = x$.



Press **menu** A: Construction | 6: Locus

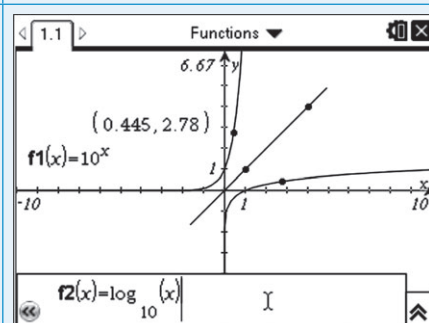
Use the touch pad to select each of the points. The calculator will display the locus of the reflection as the point moves along the curve.



Click in the entry line at the bottom of the work area. " $f2(x)=$ " is displayed.

Type $\log_{10}(x)$ and press **enter**.

The reflected curve and the logarithmic function coincide, showing that $y = \log_{10}x$ is inverse of the function $y = 10^x$.



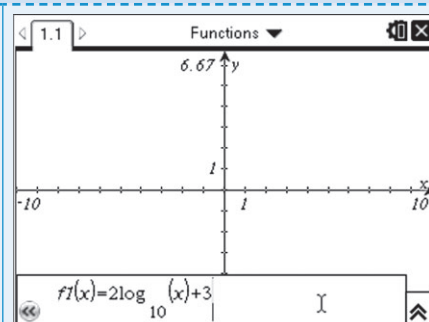
1.18 Drawing a logarithmic graph

Example 21

Draw the graph of $y = 2\log_{10}x + 3$.

Open a new document and add a Graphs page.

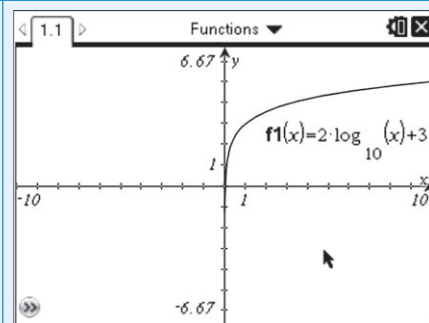
The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form " $f1(x)=$ " is displayed. The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



Type $2\log_{10}(x) + 3$ and press **enter**.

(**Note:** Type **2** **ctrl** **log** and enter 10 as the base of the logarithm. Enter x in the argument section of the template, use the **►** to move beyond the brackets to enter $+3$)

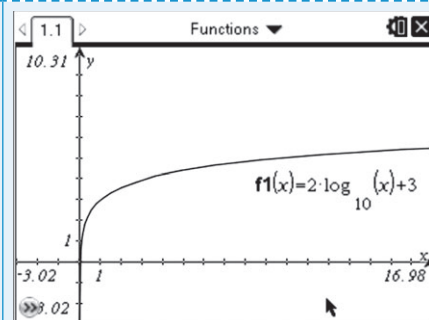
The calculator displays the curve with the default axes.



► Continued on next page

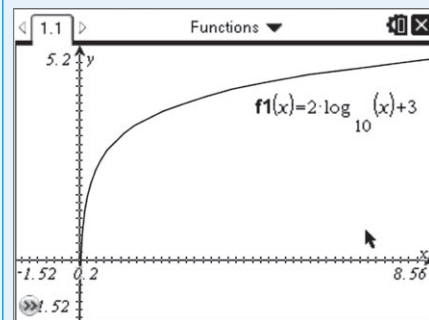
Pan the axes to get a better view of the curve.

For help with panning,
see your GDC manual.



Grab the x -axis and change it to make the logarithmic curve fit the screen better.

For help with changing
axes, see your GDC
manual.



Trigonometric functions



1.19 Degrees and radians

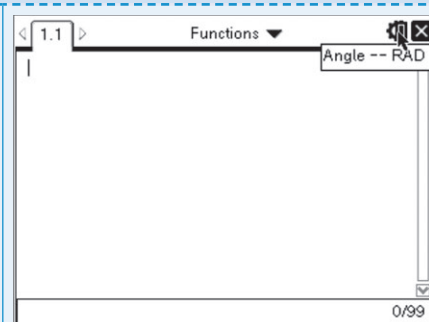
Work in trigonometry will be carried out either in degrees or radians. It is important, therefore, to be able to check which mode the calculator is in and to be able to switch back and forth. On the TI-Nspire, there are three separate settings to make: general, graphing and geometry. The defaults for general and graphing are radians and for geometry the default is degrees. Geometry is only used for drawing plane geometrical figures. Normally the two important settings are general and graphing. General refers to the angle used in calculations and graphing is for drawing trigonometric graphs.

Example 22

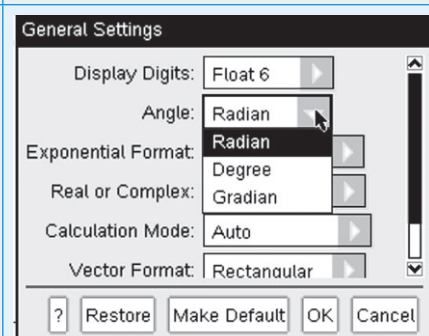
Change angle settings from radians to degrees and from degrees to radians.

Open a new document and add a Calculator page.


Move the cursor to the  symbol at the top right hand side of the screen. It will display the *general* angle mode – either radians or degrees. Click in the  symbol and choose 2:Settings | 1:General.

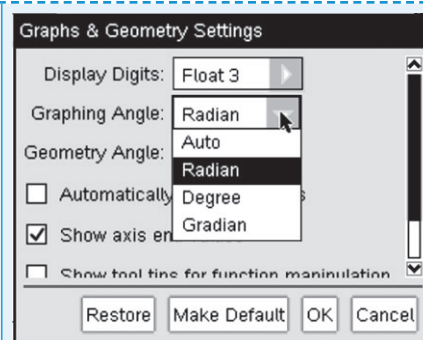


In the dialogue box, select either degrees or radians and then click on OK.



▶ Continued on next page

To change the setting for graphing, click in the  symbol and choose 2:Settings | 2:Graphs & Geometry.
In the dialogue box, select either degrees or radians for the Graphing Angle and then click on OK.




1.20 Drawing trigonometric graphs

Example 23

Draw the graph of $y = 2\sin\left(x + \frac{\pi}{6}\right) + 1$.

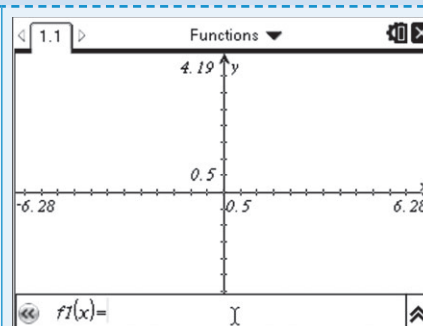
Open a new document and add a Graphs page.


Press  4:Window / Zoom | 8:Zoom - Trig


The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form " $f1(x)=$ " is displayed.

The default axes are $-6.28 \leq x \leq 6.28$ and $-4.19 \leq y \leq 4.19$.

These are the basic axes for graphing trigonometric graphs with x between -2π and 2π . If the calculator is in degree mode, the x -axis will be between -360 and 360 .



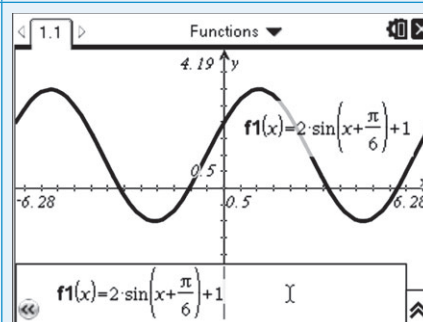
Type $y = 2\sin\left(x + \frac{\pi}{6}\right) + 1$ and press .

To enter sin, press  and choose sin from the dialogue box.

sin	cos	tan	csc	sec	cot
sin ⁻¹	cos ⁻¹	tan ⁻¹	csc ⁻¹	sec ⁻¹	cot ⁻¹


To enter π , press  and choose π from the dialogue box.



π	i	∞	e
θ	r	g	



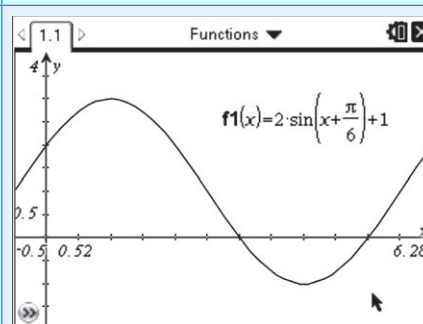
Pan the axes to get a better view of the curve and grab them to change the view.

It is also useful to change the x -axis scale to a multiple of π , such as $\frac{\pi}{6}$ as this will often show the positions of intercepts and turning points more clearly.

Change the scale by pressing  4:Window / Zoom | 1:Window Settings

XScale:  

Type $\pi/6$ in the dialogue box for XScale.



More complicated functions

1.21 Solving a combined quadratic and exponential equation

Example 24

Solve the equation $x^2 - 2x + 3 = 3 \cdot 2^{-x} + 4$

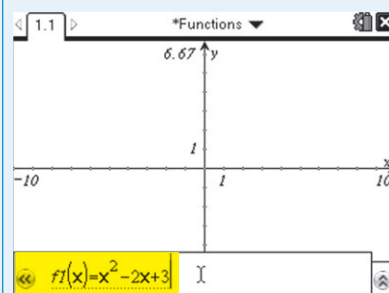
To solve the equation, find the point of intersection of the quadratic function $f1(x) = x^2 - 2x + 3$ with the exponential function $f2(x) = 3 \cdot 2^{-x} + 4$.

To draw the graphs $f1(x) = x^2 - 2x + 3$ and $f2(x) = 3 \cdot 2^{-x} + 4$:

Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x)=$ ' is displayed.

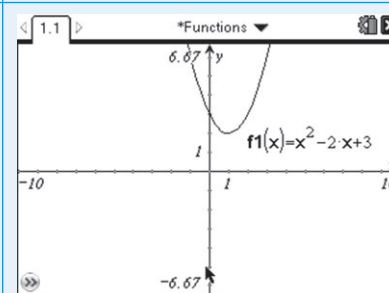
The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



Type $x^2 - 2x + 3$ and press **enter**.

The GDC displays the first curve:

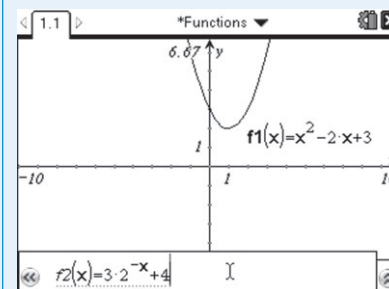
$$f1(x) = x^2 - 2x + 3$$



Use the touchpad to click on the arrows in the bottom left-hand corner of the screen.

This will open the entry line again. This time ' $f2(x)=$ ' is displayed.

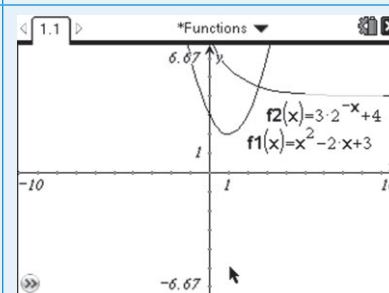
Type $3 \cdot 2^{-x} + 4$ and press **enter**.



The GDC displays both curves:

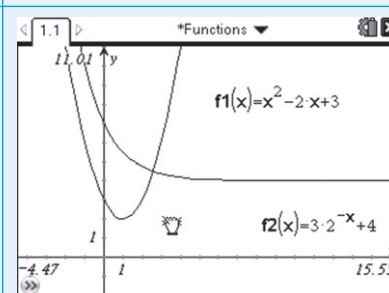
$$f1(x) = x^2 - 2x + 3$$

$$f2(x) = 3 \cdot 2^{-x} + 4$$



Pan the axes to get a better view of the curves.

For help with panning, see your GDC manual.



Continued on next page

Press **menu** 6:Analyze Graph | 4:Intersection Point(s)

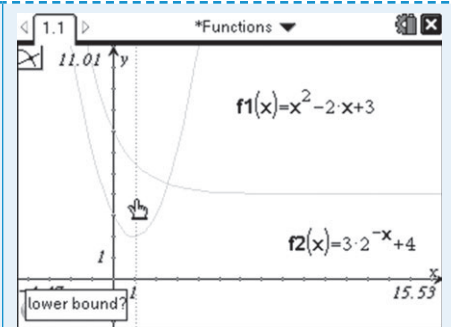
Press **enter**

To find the intersection you need to give the lower and upper bounds of a region that includes the intersection.

The GDC shows a line and asks you to set the lower bound.

Move the line using the touchpad and choose a position to the left of the intersection.

Click the touchpad.

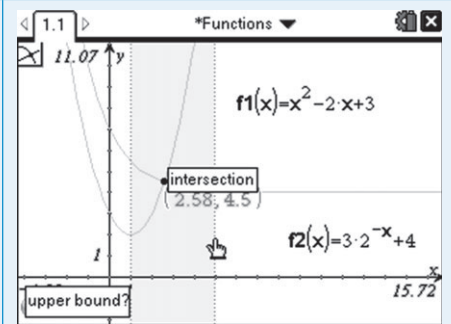


The GDC shows another line and asks you to set the upper bound.

Use the touchpad to move the line so that the region between the upper and lower bounds contains the intersection.

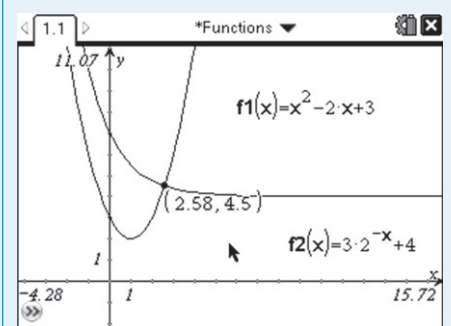
When the region contains the intersection, the calculator will display the word 'intersection' in a box.

Click the touchpad.



The GDC displays the intersection of the two curves at the point (2.58, 4.5).

The solution is $x = 2.58$.



Sequences and series

1.22 Summation of a series

Example 25

Find the sum of the first 20 terms of the arithmetic sequence 4, 7, 10, 13, ...

The k th term of an arithmetic sequence is $u_k = u_1 + (k - 1)d$

In this example $u_1 = 4$, $d = 3$ and $n = 20$.

$$S_n = \sum_{k=1}^{20} 4 + (k - 1)3.$$

Open a new document and add a calculator page.

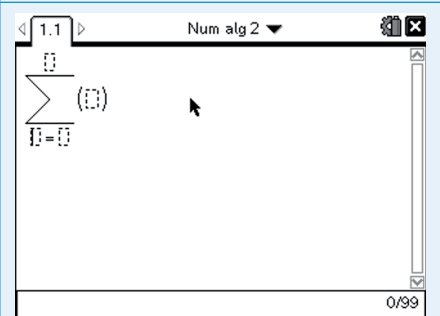
Press the template button **|||** and select the summation template using the **◀ ▶ ▼ ▲** keys and press **enter**



The template matches the written Sigma formula.

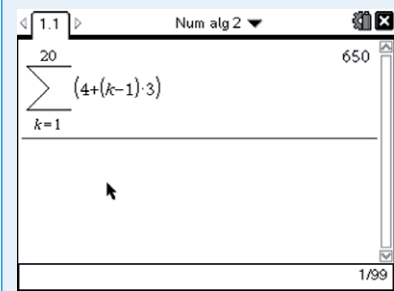
Enter the variables, values and the function as they are written.

Use the **◀ ▶ ▼ ▲** keys or the **tab** to move around the template.



▶ Continued on next page

The sum of the terms of the sequence is 650.



Example 26



Find the sum of the first 12 terms of the geometric sequence $3, -1, \frac{1}{3}, -\frac{1}{9}, \dots$

The k th term of a geometric sequence is $u_k = u_1 \cdot r^{k-1}$

In the example $u_1 = 3, r = -\frac{1}{3}$ and $n = 12$.

$$S_n = \sum_{k=1}^{12} 3 \cdot \left(-\frac{1}{3}\right)^{k-1}$$

Open a new document and add a calculator page.

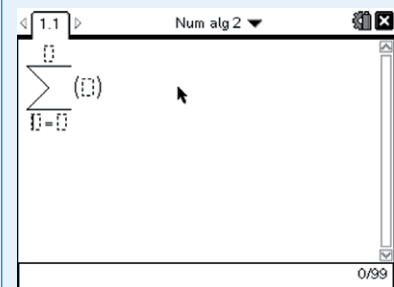
Press the template button  and select the summation template using the $\blacktriangleleft \blacktriangleright \blacktriangledown \blacktriangleup$ keys and press .



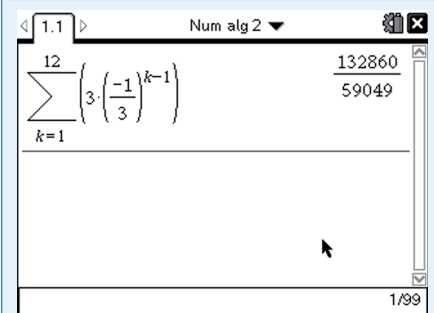
The template matches the written Sigma formula.



Enter the variables, values and the function as they are written.

Use the $\blacktriangleleft \blacktriangleright \blacktriangledown \blacktriangleup$ keys or the  to move around the template.

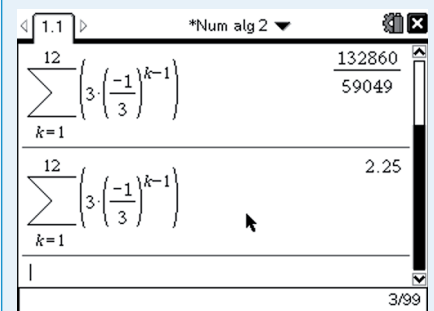


The sum of the terms of the sequence is $\frac{132860}{59049}$



The sum is given as an exact value. To change it to a decimal (approximate) value, press  .

So the sum of the terms of sequence is 2.25, to 3 significant figures.





Example 27

How many terms of the series $2 + 1\frac{1}{3} + \frac{8}{9} + \frac{16}{27} + \dots$ are needed before their sum exceeds 5.5?

In the example $u_1 = 2$, $r = \frac{2}{3}$ and n is to be found. $S_n = \sum_{k=1}^n 2 \cdot \left(\frac{2}{3}\right)^{k-1}$

Open a new document and add a calculator page.

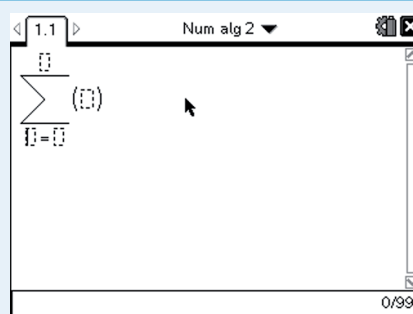
Press the template button  and select the summation template using the $\blacktriangleleft \blacktriangleright \blacktriangledown \blacktriangleup$ keys and press .



The template matches the written Sigma formula.

Enter the variables, values and the function as they are written.

Use the $\blacktriangleleft \blacktriangleright \blacktriangledown \blacktriangleup$ keys or the  to move around the template.



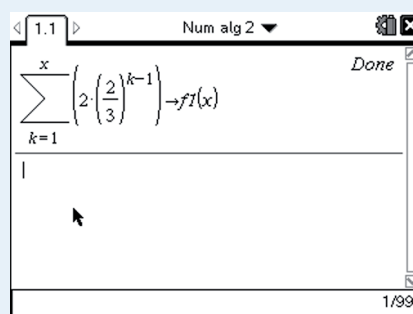
In place of the value for n type x .

Type the Sigma formula for the series.

Press   and type $f1(x)$

Press .

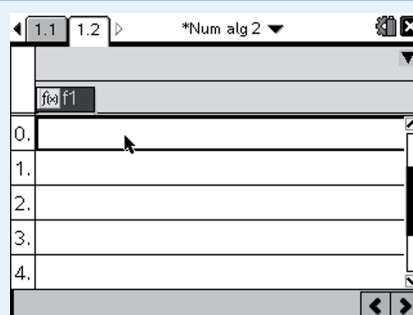
This stores the Sigma formula as the function $f1(x)$ in the same way as if you had typed it into the entry line in a graphs page.



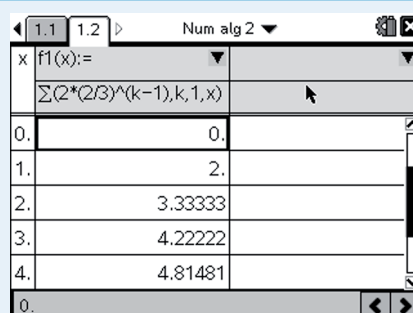
Instead of looking at the function as a graph, you will look at it in a table.

Press  and open a new Lists & Spreadsheet page.

Press  .



You will see a list of the sums of the series for different values of x .



► Continued on next page

Scrolling down the table shows that when $n = 7$, $S_n > 5.5$ as required.

x	f1(x):=
	$\Sigma(2*(2/3)^{(k-1)}, k, 1, x)$
3.	4.22222
4.	4.81481
5.	5.20988
6.	5.47325
7.	5.64883
5.6488340192044	

Modelling

1.23 Using sinusoidal regression

The notation $\sin^2 x$, $\cos^2 x$, $\tan^2 x$, ... is a mathematical convention that has little algebraic meaning. To enter these functions on the GDC, you *should* enter $(\sin(x))^2$, etc. However, the calculator will conveniently interpret $\sin(x)^2$ and translate it as $(\sin(x))^2$.

Example 28

It is known that the following data can be modeled using a sine curve.

x	0	1	2	3	4	5	6	7
y	6.9	9.4	7.9	6.7	9.2	8.3	6.5	8.9

Use sine regression to find a function to model this data.

Open a new document and add a Lists & Spreadsheet page.

Type 'x' in the first cell and 'y' in the cell to its right.

Type the numbers from the x-list in the first column and those from the y-list in the second.

Use the \blacktriangledown \blacktriangleleft \blacktriangleright keys to navigate around the spreadsheet.

	x	y
1	0	6.9
2	1	9.4
3	2	7.9
4	3	6.7
5	4	9.2

Press On and add a new graphs page to your document.

Press menu 3:Graph Type | 4:Scatter Plot

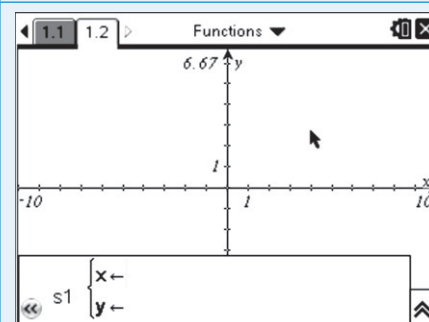
Press enter

The entry line is displayed at the bottom of the work area. Scatter plot type is displayed.

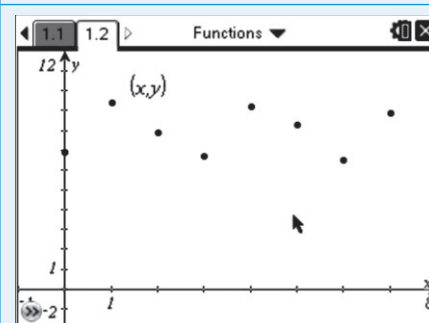
Enter the names of the lists, x and y, into the scatter plot function

Use the tab key to move from x to y.

Press enter del



Adjust your window settings to show your data and the x- and y-axes. You now have a scatter plot of x against y.



▶ Continued on next page

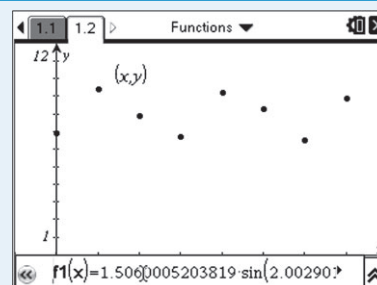
Press **ctrl** **◀** to return to the Lists & Spreadsheet page.
 Select an empty cell and press **menu** 4:Statistics | Stat Calculations | C:Sinusoidal Regression...
 Press **enter**
 From the drop down menus choose 'x' for X List and 'y' for Y List. You should press **tab** to move between the fields.
 Press **enter**

On screen, you will see the result of the sinusoidal regression in lists next to the lists for x and y .
 The equation is in the form $y = a\sin(bx + c) + d$ and you will see the values of a , b , c and d displayed separately.
 The equation of the sinusoidal regression line is
 $y = 1.51\sin(2.00x - 0.80) + 7.99$

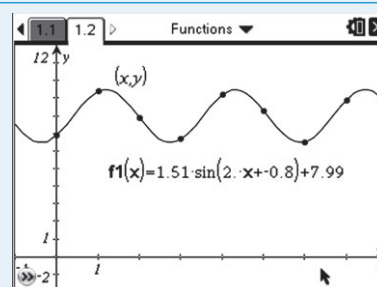
	x	y		
1	0	6.9	Title	Sinusoid...
2	1	9.4	RegEqn	a*sin(b*x...
3	2	7.9	a	1.506
4	3	6.7	b	2.0029
5	4	9.2	c	-0.799874

D1 = "Sinusoidal Regression"

Press **ctrl** **▶** to return to the Graphs page.
 Using the touchpad, click on **2** to open the entry line at the bottom of the work area.
 You will see that the equation of the regression line has been pasted into $f1(x)$.
 Press **enter**



The regression line is now shown on the graph.



1.24 Using transformations to model a quadratic function

Example 29

This data is approximately connected by a quadratic function.

x	-2	-1	0	1	2	3	4
y	9.1	0.2	-4.8	-5.9	-3.1	4.0	15.0

Find a function that fits the data.

Open a new document and add a Lists & Spreadsheet page.
 Enter the data in two lists:
 Type 'x' in the first cell and 'y' in the cell to its right.
 Enter the x -values in the first column and the y -values in the second.
 Remember to use **(-)** to enter a negative number.
 Use the **▼** **▲** **◀** **▶** keys to navigate around the spreadsheet.

	x	y
1	-2	9.1
2	-1	0.2
3	0	-4.8
4	1	-5.9
5	2	-3.1

You can also model a linear function by finding the equation of the least squares regression line (see section 5.16).

Transform a basic quadratic curve to find an equation to fit some quadratic data.

Continued on next page

Add a Graphs page to your document.

Press **menu** 3:Graph Type | 4:Scatter Plot

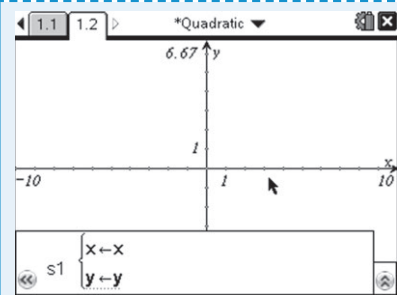
Press **enter**

The entry line is displayed at the bottom of the work area. Scatter plot type is displayed.

Enter the names of the lists, x and y , into the scatter plot function.

Use the **tab** key to move from x to y .

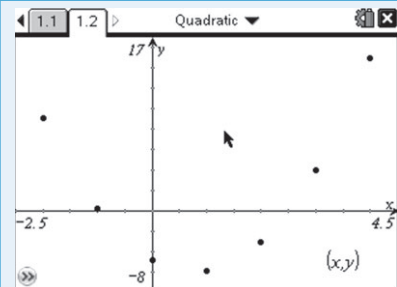
Press **enter**



Press **menu** A:Zoom – Fit from the Window/Zoom menu

This is a quick way to choose an appropriate scale to show all the points.

You should recognize that the points are in the shape of a quadratic function.



The next step is to enter a basic quadratic function, $y = x^2$, and manipulate it to fit the points.

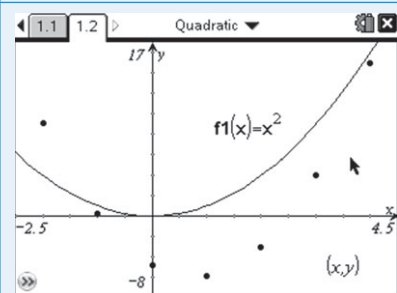
Press **menu** 3:Graph Type | 1:Function

Press **enter**

This changes the graph type from scatter plot to function.

Type x^2 in as function $f1(x)$.

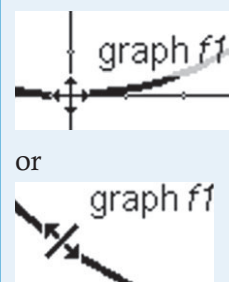
It is clear that the curve does not fit any of the points, but it is the right general shape to do so.



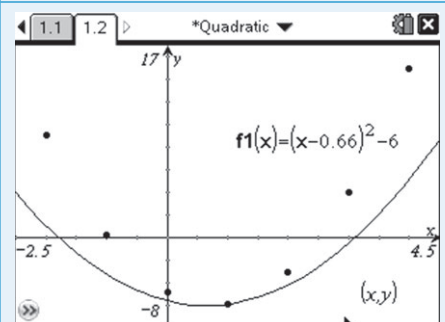
Use the touchpad to move the cursor so it approaches the curve. You will see one of two icons.

The first will allow you to drag the quadratic function around the screen by its vertex.

The second allows you to stretch the function either vertically or horizontally.



Use \updownarrow to position the vertex where you think it ought to be according to the data points.

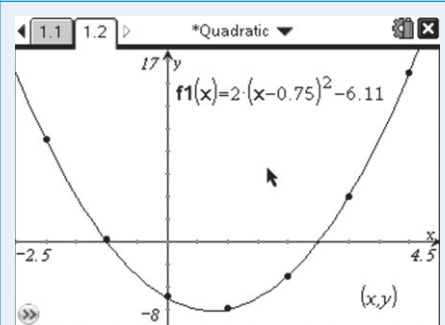


Use \times to adjust the stretch of the curve.

Make some final fine adjustments using both the tools until you have a good fit to the data points.

The equation of the function that fits the data is:

$$f1(x) = 2(x - 0.75)^2 - 6.11$$



1.25 Using sliders to model an exponential function

Example 30

In general, an exponential function has the form $y = ka^x + c$.

For this data, it is known that the value of a is 1.5, so $y = k(1.5)^x + c$.

x	-3	-2	-1	0	1	2	3	4	5	6	7	8
y	3.1	3.2	3.3	3.5	3.8	4.1	4.7	5.5	6.8	8.7	11.5	15.8

Find the values of the constants k and c .

Open a new document and add a Lists & Spreadsheet page.

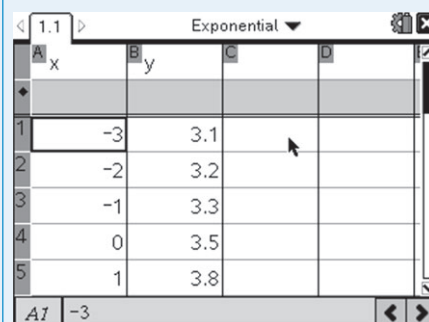
Enter the data in two lists:

Type ' x ' in the first cell and ' y ' in the cell to its right.

Enter the x -values in the first column and the y -values in the second.

Remember to use $(-)$ to enter a negative number.

Use the \blacktriangleleft \blacktriangleright $\blacktriangleleft\blacktriangleright$ keys to navigate around the spreadsheet.



Add a Graphs page to your document.

Press menu 3:Graph Type | 4:Scatter Plot

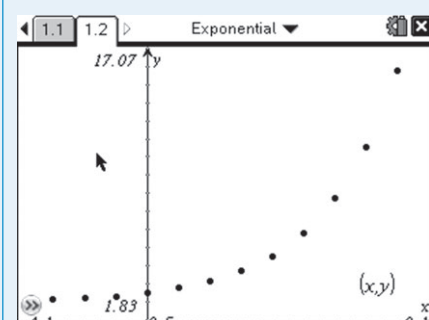
Press enter

The entry line is displayed at the bottom of the work area. Scatter plot type is displayed.

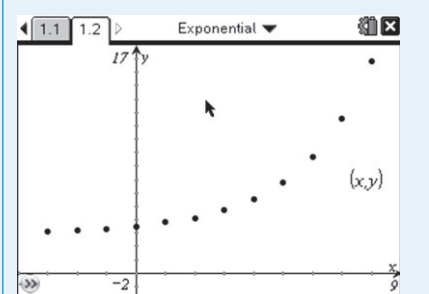
Enter the names of the lists, x and y , into the scatter plot function.

Use the tab key to move from x to y .

Press enter



Adjust the window settings to fit the data and to display the axes clearly.

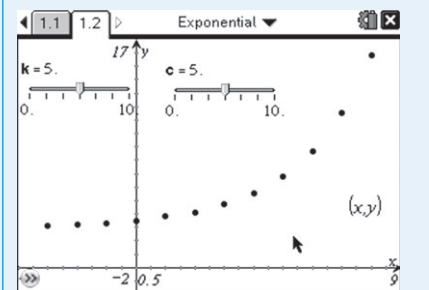


Press menu I:Actions | A:Insert Slider

Position the slider somewhere where it is not in the way and change the name of the constant to k .

Repeat and add a second slider for c .

For help with sliders,
see your GDC manual.



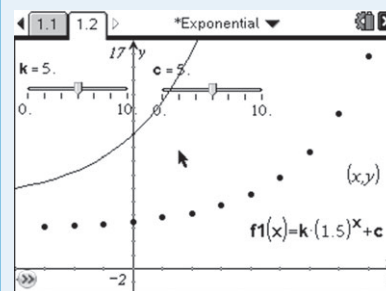
► Continued on next page

Press **menu** 3:Graph Type | 1:Function

Press **enter**

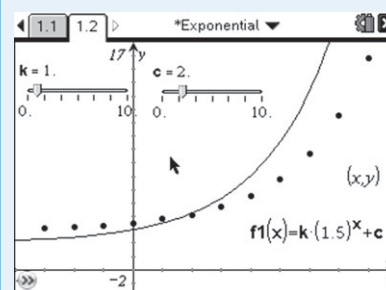
This changes the graph type from scatter plot to function.

Type $k(1.5)^x + c$ in as function $f1(x)$.



Try adjusting the sliders.

You can get the curve closer to the points but they are not sufficiently adjustable to get a good fit.



You can change the slider settings by selecting the slider, pressing **ctrl**

menu and selecting 1:Settings.

Change the default values for k to:

Minimum 0

Maximum 2

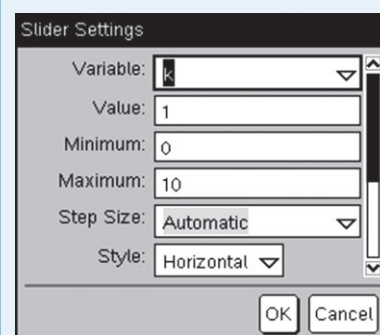
Step Size 0.1

Change the default values for c to:

Minimum 0

Maximum 4

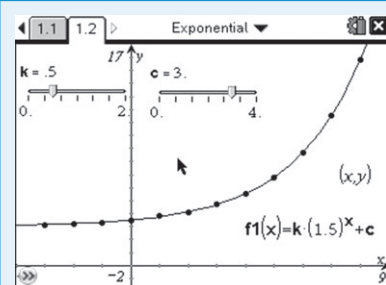
Step Size 0.1



You can now adjust the sliders to get a much better fit to the curve.

The screen shows the value of k is 0.5 and c is 3.

So the best fit for the equation of the function is approximately $y = 0.5(1.5)^x + 3$.



1.26 Drawing a piecewise function

Example 31

Draw the function $f(x) = \begin{cases} x^2 - 4x + 3, & x < 3 \\ \frac{1}{2}(x - 3), & x \geq 3 \end{cases}$

Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form $f1(x)=$ is displayed.

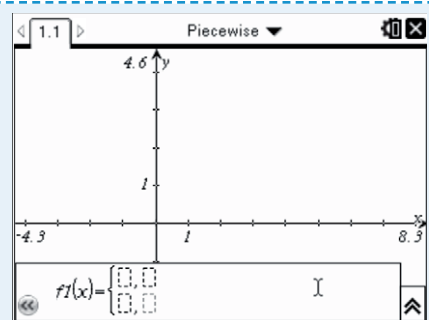
Press **|=|** and select the two-piece piecewise function template.



► Continued on next page

The spaces in the template are for the two functions and their domains.

Enter the variables, values and the function as they are written.

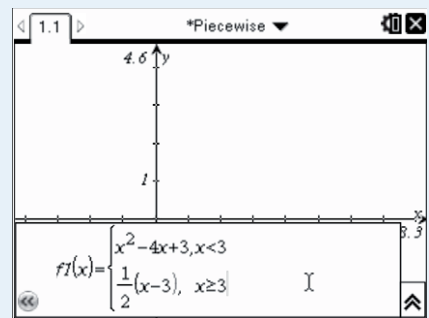


Use the \leftarrow \rightarrow \uparrow \downarrow keys or the **tab** to move around the template.

To enter the inequalities for the domain use **ctrl** $\left[\right]$.

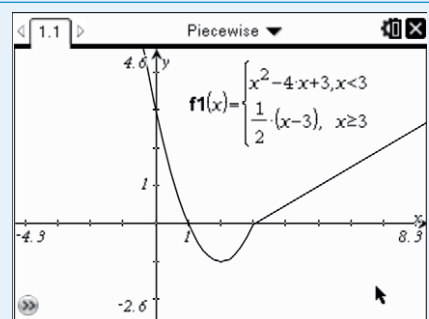
Press **enter**.

Choose suitable axes to display the curves.



The piecewise function is displayed.

By using the n -piece piecewise template, more complicated piecewise functions can be drawn.



2 Differential calculus

2.1 Finding the gradient at a point

Example 32

Find the gradient of the cubic function $y = x^3 - 2x^2 - 6x + 5$

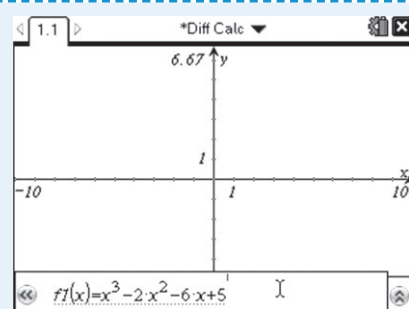
Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form ' $f1(x)=$ ' is displayed.

The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.

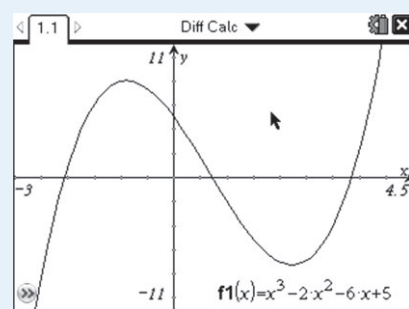
Type $x^3 - 2x^2 - 6x + 5$ and press **enter**.

Note: Type \times \wedge 3 \rightarrow to enter x^3 . The \rightarrow returns you to the baseline from the exponent.



Pan the axes to get a better view of the curve and then grab the x - and y -axes to fit the curve to the window.



For help with panning and changing axes, see your GDC manual.



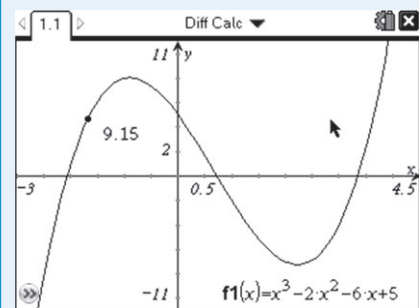
► Continued on next page


Press **menu** 6:Analyze Graph | 5: $\frac{dy}{dx}$

Press **enter**

Using the touchpad, move the  towards the curve. As it approaches the curve, it turns to  and displays the numerical value of the gradient.

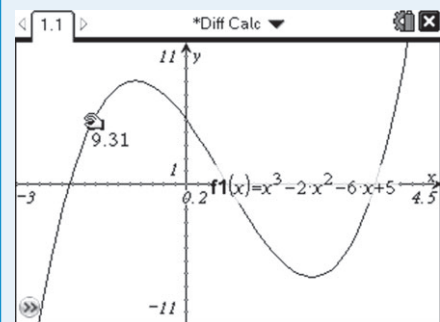
Press **enter** to attach a point on the curve.



Use the touchpad to move the  icon to the point.

You can move the point along the curve and observe how the gradient changes as the point moves.

Here, gradient at point = 9.31.

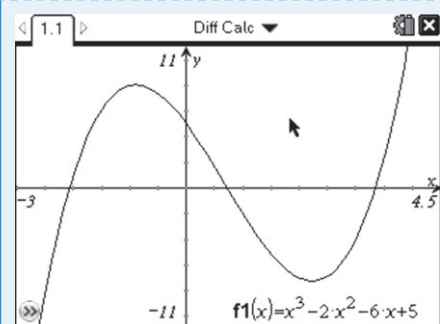


2.2 Drawing a tangent to a curve

Example 33



Draw a tangent to the curve $y = x^3 - 2x^2 - 6x + 5$

First draw the graph of $y = x^3 - 2x^2 - 6x + 5$ (see Example 32).



Press **menu** 7:Points & Lines | 7:Tangent

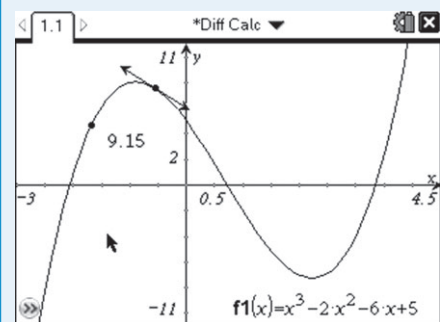
Press **enter**

Using the touchpad, move the  towards the curve. As it approaches the curve, it turns to .

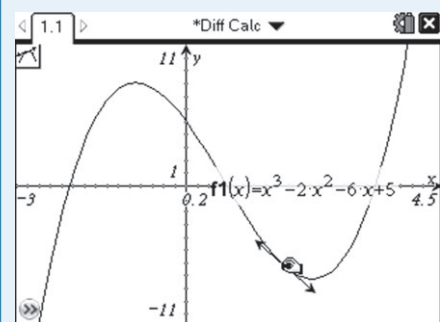
Press **enter**

The cursor changes to  and displays 'point on'.

Choose a point where you want to draw a tangent and press **enter**.



You can move the point that the tangent line is attached to with the touchpad.



► Continued on next page

Use the touchpad to drag the arrows at each end of the tangent line to extend it.

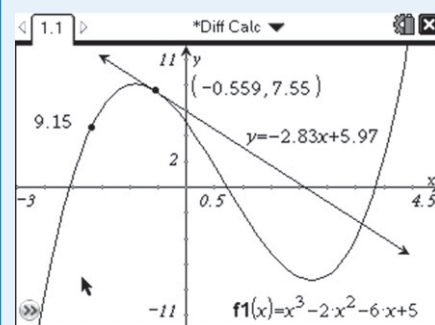
Press **ctrl** **menu** with the tangent line selected – move to the arrow at the end and look for the word ‘line’.

Choose 7:Coordinates and Equations

Click on the line to display the equation of the tangent:

$$y = -2.83x + 5.97.$$

Click on the point to display the coordinates of the point: $(-0.559, 7.55)$.



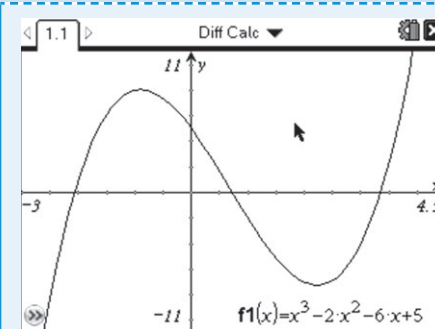
2.3 Finding maximum and minimum points

Example 34

Find the local maximum and local minimum points on the cubic curve:

$$y = x^3 - 2x^2 - 6x + 5$$

First draw the graph of $y = x^3 - 2x^2 - 6x + 5$ (see Example 32).



Press **menu** 6:Analyze Graph | 2:Minimum

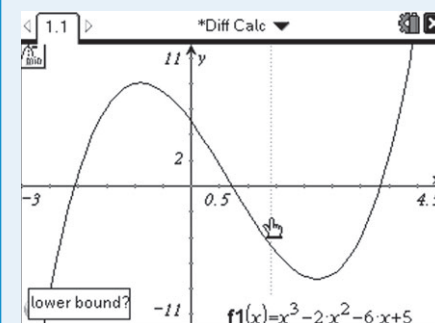
Press **enter**

To find the minimum you need to give the lower and upper bounds of a region that includes the minimum.

The GDC shows a line and asks you to set the lower bound.

Move the line using the touchpad and choose a position to the left of the minimum.

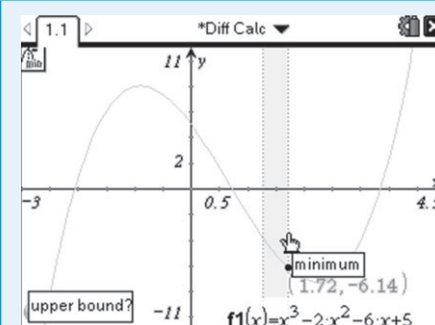
Click the touchpad.



The GDC shows another line and asks you to set the upper bound.

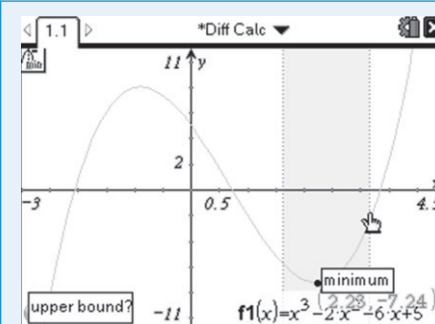
Use the touchpad to move the line so that the region between the upper and lower bounds contains the minimum.

Note: The minimum point in the region that you have defined is being shown. In this screenshot it is not the local minimum point. Make sure you move the line beyond the point you are looking for.



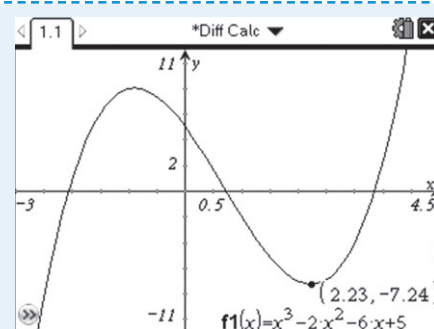
When the region contains the minimum, the GDC will display the word ‘minimum’ in a box and a point that lies between the lower and upper bounds. The point displayed is clearly between the upper and lower bounds.

Click the touchpad.

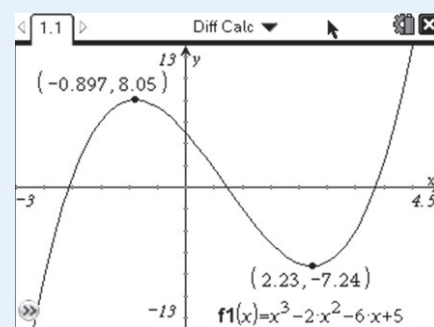


▶ Continued on next page

The GDC displays the local minimum at the point $(2.23, -7.24)$.



Press **menu** 6:Analyze Graph | 3:Maximum to find the local maximum point on the curve in exactly the same way.
The maximum point is $(-0.897, 8.05)$.



2.4 Finding a numerical derivative

Using the calculator it is possible to find the numerical value of any derivative for any value of x . The calculator will not, however, differentiate a function algebraically. This is equivalent to finding the gradient at a point graphically (see Section 2.1 example 32).

Example 35

If $y = \frac{x+3}{x}$, evaluate $\frac{dy}{dx}|_{x=2}$

Open a new document and add a Calculator page.

Press **menu** 4:Calculus | 1:Numerical Derivative at a Point...

Leave the variable as x and the Derivative as 1st Derivative. Change the Value to the value of x at which you wish to evaluate the derivative, in this case $x = 2$.

Numerical Derivative at a Point

Variable:

Value:

Derivative:

OK **Cancel**

Enter the function in the template.

Press **enter**

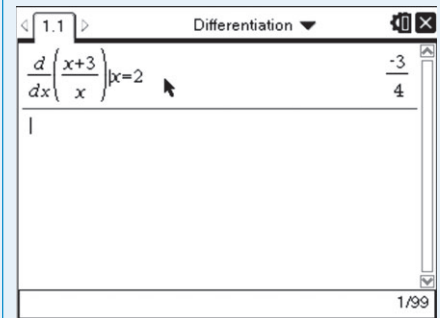
1.1 **Differentiation**

$\frac{d}{dx}(\frac{x+3}{x})|_{x=2}$

0/99

► Continued on next page

The calculator shows that the value of the first derivative of $y = \left(\frac{x+3}{x}\right)$ is $-\frac{3}{4}$ when $x = 2$.



2.5 Graphing a numerical derivative

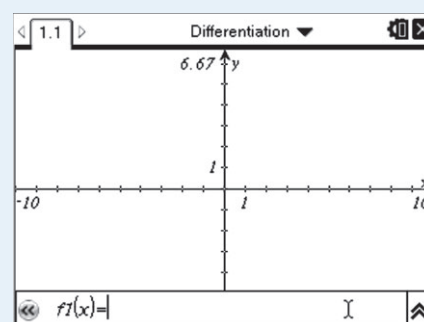
Although the calculator can only evaluate a numerical derivative at a point, it will graph the gradient function for all values of x .


Example 36

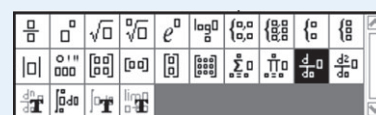
If $y = \frac{x+3}{x}$, draw the graph of $\frac{dy}{dx}$.


Open a new document and add a Graph page.

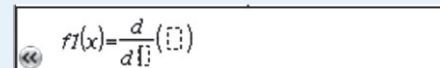
The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form " $f1(x)=$ " is displayed. The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.



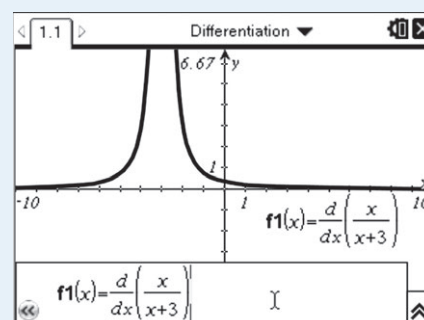
Press the templates button marked  and choose the numerical derivative.



In the template enter x and the function $\frac{x+3}{x}$.
Press .



The calculator displays the graph of the numerical derivative function of $y = \frac{x+3}{x}$.



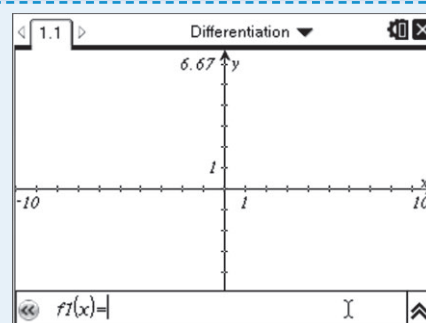
Example 37


Find the values of x on the curve $y = \frac{x^3}{3} + x^2 - 5x + 1$ where the gradient is 3.

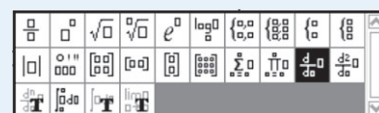
Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form " $f1(x) =$ " is displayed.

The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.

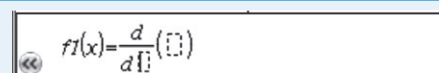


Press the templates button marked  and choose the numerical derivative.

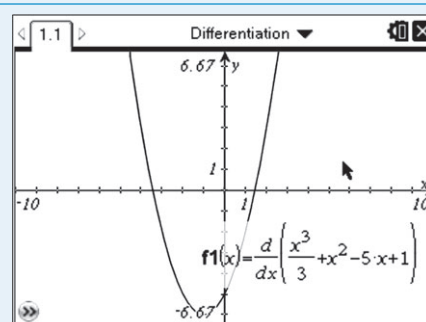



In the template enter x and the function $\frac{x^3}{3} + x^2 - 5x + 1$.

Press .



The calculator displays the graph of the numerical derivative function of $y = \frac{x^3}{3} + x^2 - 5x + 1$.

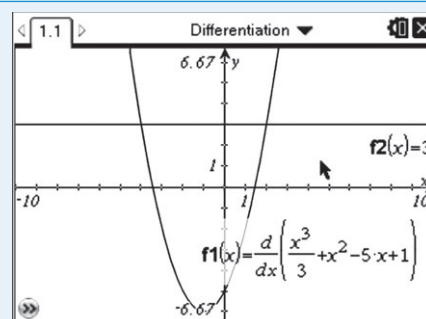


Using the touchpad, click on  to open the entry line at the bottom of the work area.

Enter the function $f2(x) = 3$

Press .

The calculator now displays the curve and the line $y = 3$.

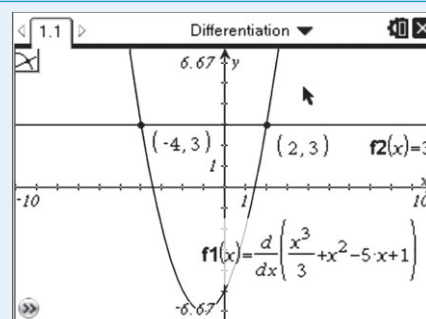


Press  7:Points & Lines | 3:Intersection Point(s)

Using the touchpad, select graph $f1$ and graph $f2$.

The calculator displays the coordinates of the intersection points of the gradient function and the line $y = 3$.

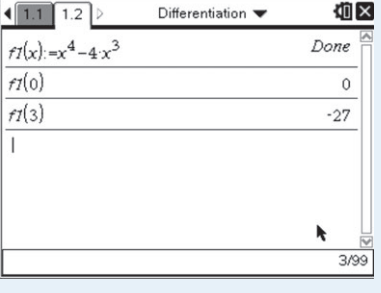
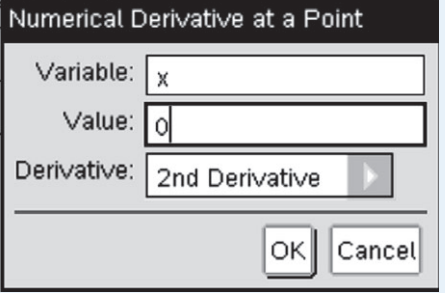
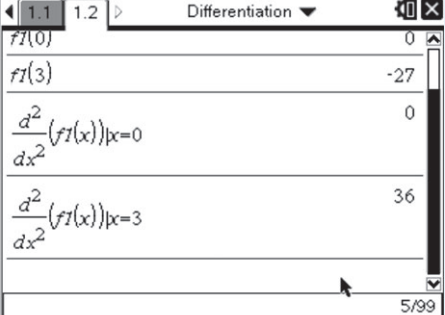
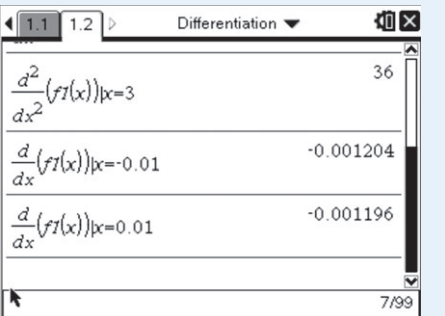
The curve has gradient 3 when $x = -4$ and $x = 2$



2.6 Using the second derivative

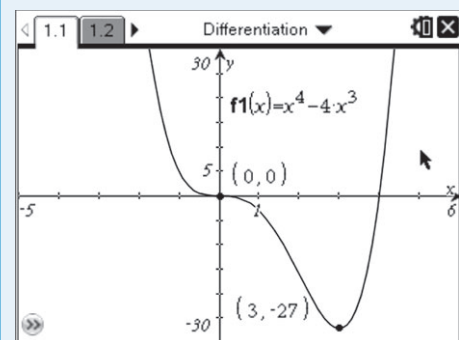
The calculator can find first and second derivatives. The second derivative can be used to determine whether a point is a maximum or minimum point.

Example 38

<p>Find the stationary points on the curve $f(x) = x^4 - 4x^3$ and determine their nature.</p> $f(x) = x^4 - 4x^3$ $f'(x) = 4x^3 - 12x^2$ <p>At stationary points</p> $f'(x) = 0$ $4x^3 - 12x^2 = 0$ $4x^2 - (x - 3) = 0$ <p>Therefore $x = 0$ or $x = 3$</p>	
<p>Use the calculator to find the coordinates of the points and to determine their nature.</p> <p>Open a new document and add a Calculator page.</p> <p>Define the function $f1(x)$</p> <p>Type F 1 (X) ctrl := and type the function.</p> <p>Evaluate the function when $x = 0$ and $x = 3$</p> <p>The stationary points are at $(0, 0)$ and $(3, -27)$</p>	
<p>Press menu 4:Calculus 1:Numerical Derivative at a Point...</p> <p>Leave the variable as x and choose 2nd Derivative. Change the Value to the value of x at which you wish to evaluate the derivative, in this case $x = 0$ (and $x = 3$).</p>	
<p>Enter $f1(x)$ in the template as the function.</p> <p>Repeat for the second derivative when $x = 3$</p> <p>(Note: you can cut and past the expression and change the 0 to 3)</p> <p>In this case we are not certain what the nature of the stationary point is at $(0, 0)$ but the point $(3, -27)$ is a minimum because $f''(x) > 0$</p>	
<p>Evaluate $f'(x)$ either side of $x = 0$.</p> <p>In this case using $x = -0.01$ and $x = 0.01$</p> <p>The gradient is negative either side of the stationary point.</p> <p>Hence $(0, 0)$ is a negative point of inflexion.</p>	

▶ Continued on next page

The graph on the right illustrates the curve, the minimum at $(3, -27)$ and the point of inflexion at $(0, 0)$.



3 Integral calculus

The calculator can find the values of definite integrals either on a calculator page or graphically. The calculator method is quicker, but the graphical method is clearer and shows discontinuities, negative areas and other anomalies that can arise.

3.1 Finding the value of a definite integral

Example 39

Evaluate $\int \left(x - \frac{3}{\sqrt{x}} \right) dx$

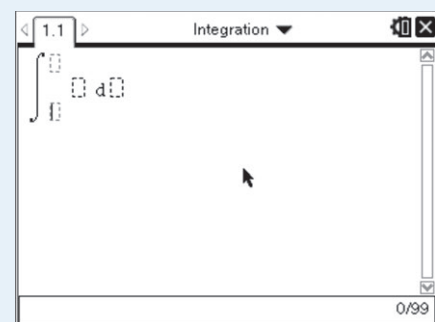
Open a new document and add a Calculator page.

Press **menu** 4:Calculus | 1:Numerical Integral...

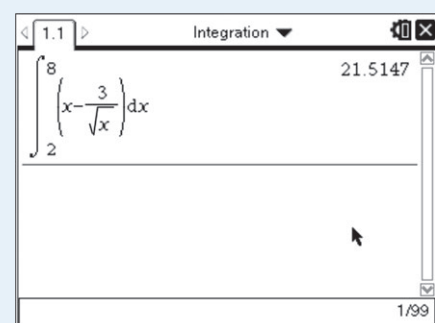
Enter the upper and lower limits, the function and x in the template.

Use the **▼ ▲ ◀ ▶** keys to navigate around the template.

In this example you will also use templates to enter the rational function and the square root.



The value of the integral is 21.5 (to 3 sf)



3.2 Finding the area under a curve

Example 40

Find the area bounded by the curve $y = 3x^2 - 5$, the x -axis and the lines $x = -1$ and $x = 1$.

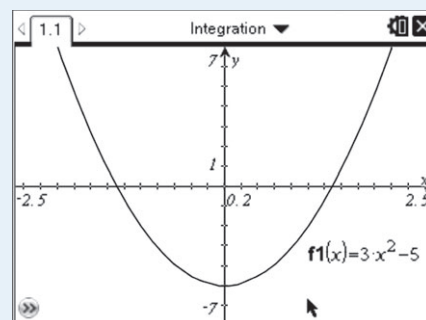
Open a new document and add a Graphs page.

The entry line is displayed at the bottom of the work area. The default graph type is Function, so the form " $f1(x)=$ " is displayed.

The default axes are $-10 \leq x \leq 10$ and $-6.67 \leq y \leq 6.67$.

Type the function $3x^2 - 5$

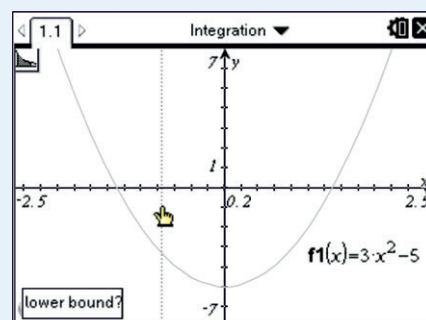
Press **enter**



Press **menu** 6:Analyze Graph | 6:Integral

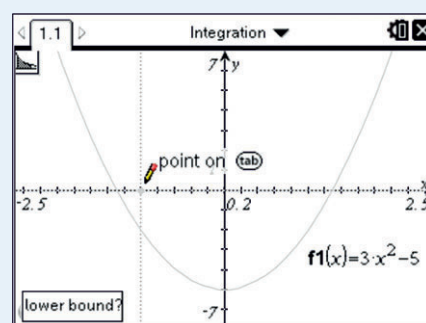
The calculator prompts you to enter the lower limit for the integral. There are several ways to do this.

You can click manually. This is not very accurate, however, and you will need to add the coordinates of the point you entered and edit them to obtain an accurate figure.



You can use the points on the axis.

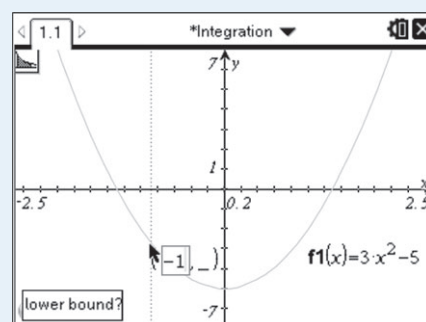
Here the scale was set to 0.2, so the point $(-1, 0)$ can be selected as shown.



You can enter the point with the keyboard.

Enter a left bracket **(** and then type **(-)** **1** and press **enter**

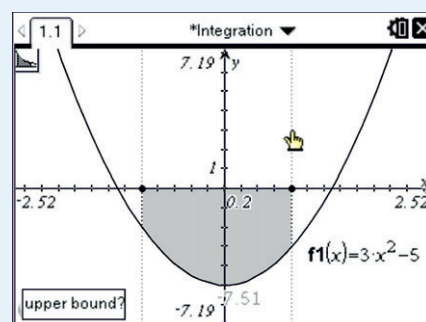
There is no need to complete the coordinates.



Repeat for the upper limit.

The calculator displays a changing value for the area.

Using one of the methods above, select a point where the value of x is 1.



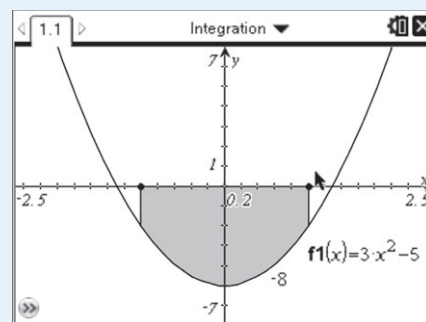
▶ Continued on next page

Repeat for the upper limit.

The area found is shaded and the value of the integral (-8) is shown on the screen.

Note: since the area lies below the x -axis in this case, the integral is negative.

The required area is 8.



4 Vectors

Scalar product

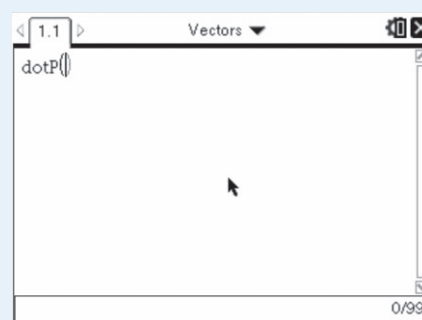
4.1 Calculating a scalar product

Example 41

Evaluate the scalar products:

a $\begin{pmatrix} 1 \\ 3 \end{pmatrix} \cdot \begin{pmatrix} -3 \\ 4 \end{pmatrix}$ **b** $\begin{pmatrix} 1 \\ -1 \\ 4 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ 2 \\ -1 \end{pmatrix}$

a Open a new document and add a Calculator page.
Press 7: Matrix & Vector | C: Vector | 3: Dot Product
(or type DOTP()).



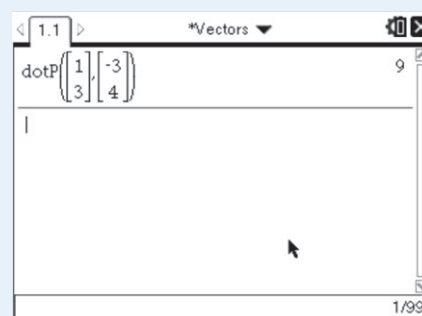
Press and choose the 2×1 column vector template.



Enter the vector type , and enter the second vector.

Press

$$\begin{pmatrix} 1 \\ 3 \end{pmatrix} \cdot \begin{pmatrix} -3 \\ 4 \end{pmatrix} = 9$$

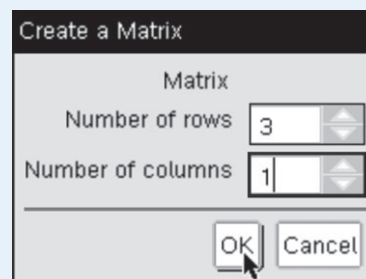


b Press 7: Matrix & Vector | C: Vector | 3: Dot Product
Press and choose the matrix template



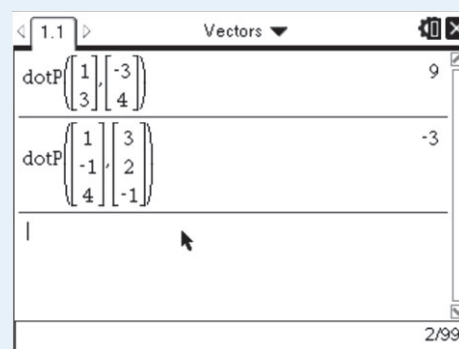
► Continued on next page

Choose 3 rows and 1 column and then click on OK.

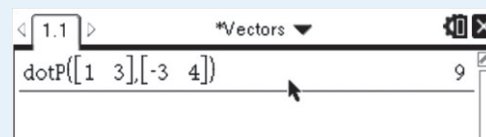
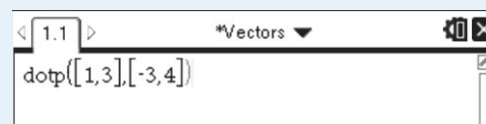


Enter the vector type, and enter the second vector.
Press

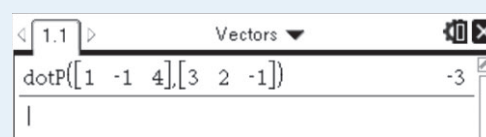
$$\begin{pmatrix} 1 \\ -1 \\ 4 \end{pmatrix} \cdot \begin{pmatrix} 3 \\ 2 \\ -1 \end{pmatrix} = -3$$



You can also enter vectors as rows by typing them in directly instead of using the templates. Separate the values in the vector with commas. When you press **enter**, the GDC changes the entry line and calculates the result.



This method can be quicker, especially with 3×1 vectors.





4.2 Calculating the angle between two vectors

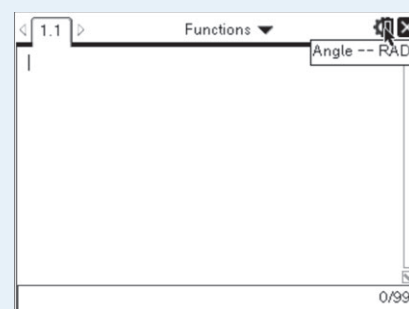
The angle θ between two vectors **a** and **b**, can be calculated using the formula

$$\theta = \arccos\left(\frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}| |\mathbf{b}|}\right)$$

Example 42

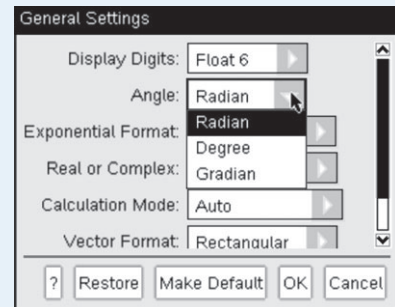
Calculate the angle between $2\mathbf{i} + 3\mathbf{j}$ and $3\mathbf{i} - \mathbf{j}$

Open a new document and add a Calculator page.
Move the cursor to the  symbol at the top right-hand side of the screen. It will display the general angle mode – either radians or degrees.
Click in the  symbol and choose 2:Settings | 1:General.

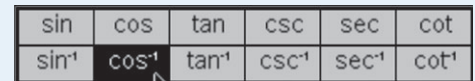


► Continued on next page

In the dialogue box, select either degrees or radians (according to the units you need your answer in) and then click on OK.

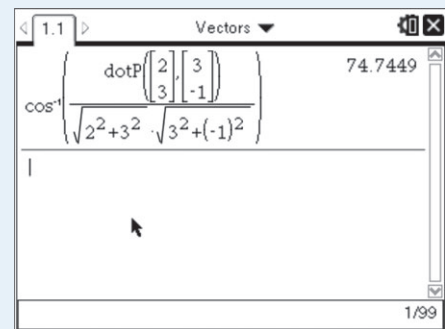


Press μ and choose \cos^{-1} from the menu.



Enter the values in the formula as shown, using the fraction template and the 2×1 column vector template.

To calculate the magnitudes of the vectors use the formula $|a\mathbf{i} + b\mathbf{j}| = \sqrt{a^2 + b^2}$

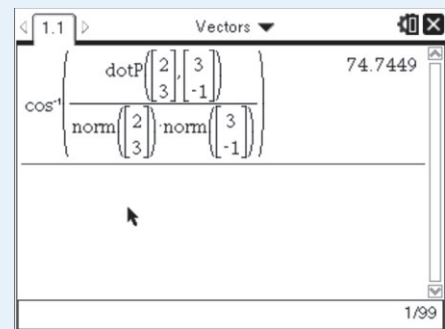


As an alternative to using the formula for the magnitude of a vector, you can use the norm function.

Press menu 7: Matrix & Vector | 7: Norms | 1: Norm

Or simply typing norm(

Instead of retyping the vectors, you can use ctrl C and ctrl V to cut and paste.



Vector product

The calculator can find the values of definite integrals either on a calculator page or graphically. The calculator method is quicker, but the graphical method is clearer and shows discontinuities, negative areas and other anomalies that can arise.

4.3 Calculating a vector product

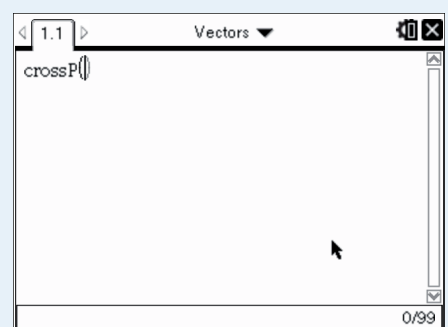
Example 43

Evaluate the vector product $\begin{pmatrix} 2 \\ -1 \\ 5 \end{pmatrix} \times \begin{pmatrix} 2 \\ 3 \\ -4 \end{pmatrix}$

Open a new document and add a Calculator page.

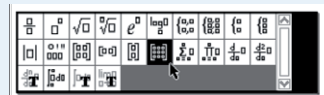
Press menu 7: Matrix & Vector | C: Vector | 2: Cross Product

Or type crossP(

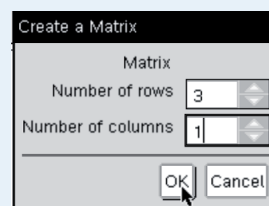


▶ Continued on next page

Press $\left[\begin{smallmatrix} \square & \square \\ \square & \square \end{smallmatrix} \right]$ and choose the matrix template.



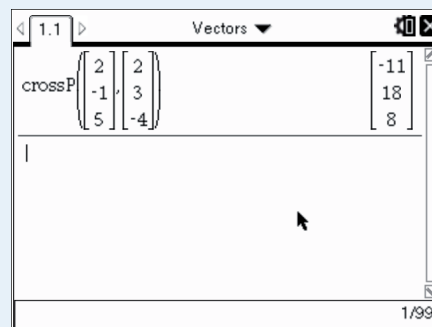
Choose 3 rows and 1 column and then click on OK.



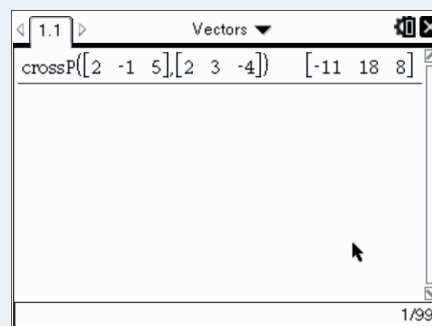
Enter the vector type and enter the second vector.

Press enter

$$\begin{pmatrix} 2 \\ -1 \\ 5 \end{pmatrix} \times \begin{pmatrix} 2 \\ 3 \\ -4 \end{pmatrix} = \begin{pmatrix} -11 \\ 18 \\ 8 \end{pmatrix}$$



You can also enter vectors as rows by typing them in directly instead of using the templates. Separate the values in the vector with commas. The GDC calculates the cross product, but represents both the input vectors and the result as rows instead of columns. You should write the answer as a column.



5 Statistics and probability

You can use your GDC to draw charts to represent data and to calculate basic statistics such as mean, median, etc. Before you can do this, you need to enter the data into a list or spreadsheet. This is done in a Lists & Spreadsheet page in your document.

Entering data

There are two ways of entering data: as a list or as a frequency table.

5.1 Entering lists of data

Example 44

Enter the data in the list 1, 1, 3, 9, 2

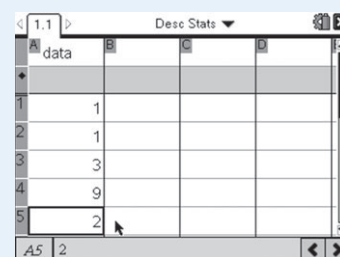
Open a new document and add a Lists & Spreadsheet page.

Type 'data' in the first cell.

Type the numbers from the list in the first column.

Press enter or \blacktriangledown after each number to move down to the next cell.

Note: The word 'data' is a label that will be used later when you want to create a chart or do some calculations with this data. You can use any letter or name to label the list.



5.2 Entering data from a frequency table

Example 45

Enter the data in a table

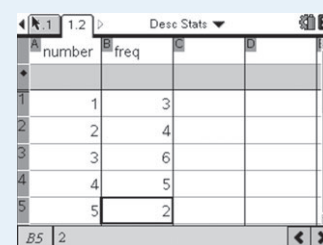
Number	1	2	3	4	5
Frequency	3	4	6	5	2

Add a new Lists & Spreadsheet page to your document.

To label the columns, type 'number' in the first cell and 'freq' in the cell to its right.

Enter the numbers in the first column and the frequencies in the second.

Use the \blacktriangledown \blacktriangle \blacktriangleleft \blacktriangleright keys to navigate around the spreadsheet.



Drawing charts

You can draw charts from a list or from a frequency table.

5.3 Drawing a frequency histogram from a list

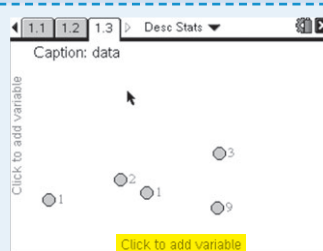
Example 46

Draw a frequency histogram for this data: 1, 1, 3, 9, 2

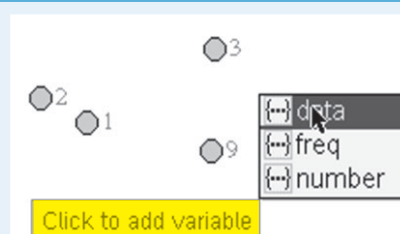
Enter the data in a list called 'data' (see Example 44).

Add a new Data & Statistics page to your document.

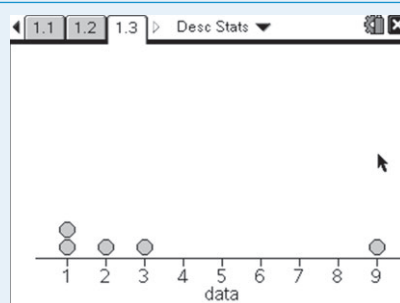
Note: You do not need to worry about what this screen shows.



Click at the bottom of the screen where it says 'Click to add variable', choose 'data' from the list and press **enter**.



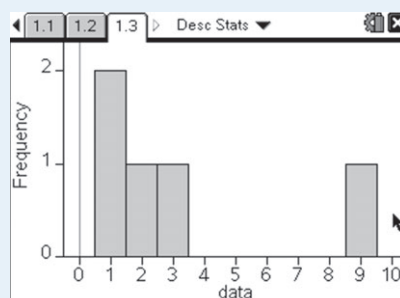
The first chart you will see is a dot plot of your data.



Press **menu** 1:Plot Type | 3:Histogram

Press **enter**

You should now see a frequency histogram for the data in the list.



5.4 Drawing a frequency histogram from a frequency table

Example 47

Draw a frequency histogram for this data:

Number	1	2	3	4	5
Frequency	3	4	6	5	2

Enter the data in lists called 'number' and 'freq'

(see Example 45).

Add a new Data & Statistics page to your document.

Note: You do not need to worry about what this screen shows.



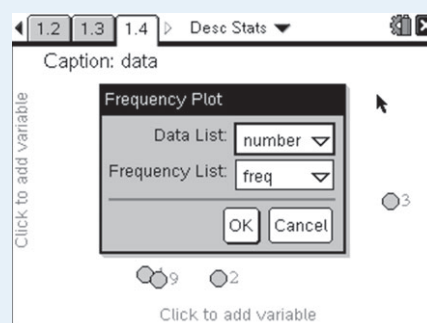
Press **menu** 2:Plot Properties | 5:Add X Variable with Frequency

Press **enter**

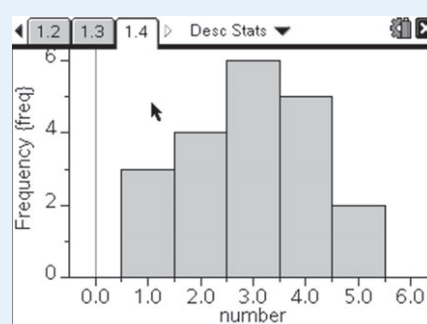
You will see this dialogue box.

From the drop-down menus, choose 'number' for the Data List and 'freq' for the Frequency List.

Press **enter**



You should now see a frequency histogram for the data in the table.



5.5 Drawing a box and whisker diagram from a list

Example 48

Draw a box and whisker diagram for this data:

1, 1, 3, 9, 2

Enter the data in a list called 'data' (see Example 44).

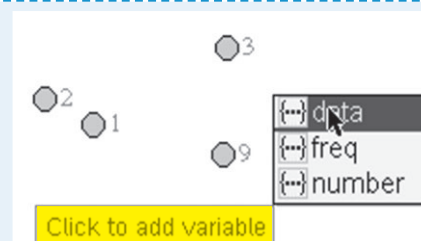
Add a new Data & Statistics page to your document.

Note: You do not need to worry about what this screen shows.

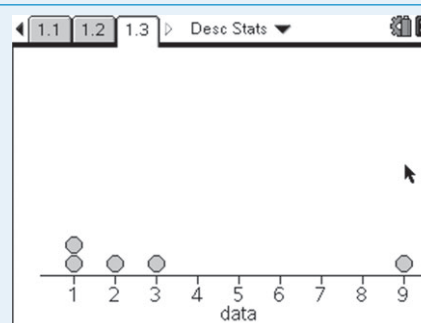


► Continued on next page

Click at the bottom of the screen where it says 'Click to add variable', choose 'data' from the list and press **enter**.



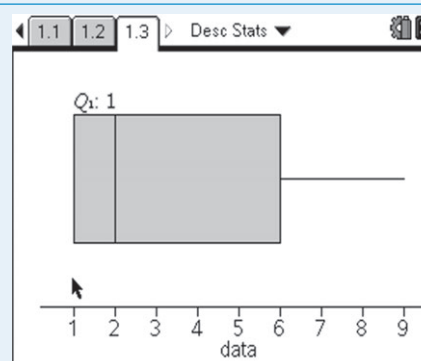
The first chart you will see is a dot plot of your data.



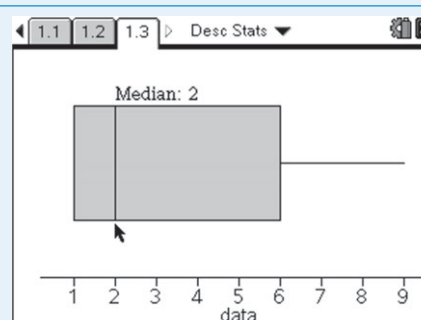
Press **menu** 1:Plot Type | 2:Box Plot

Press **enter**

You should now see a box plot (box and whisker diagram) for the data in the list.



Move the cursor over the plot and you will see the quartiles, Q_1 and Q_3 , the median, and the maximum and minimum values.



5.6 Drawing a box and whisker diagram from a frequency table

Example 49

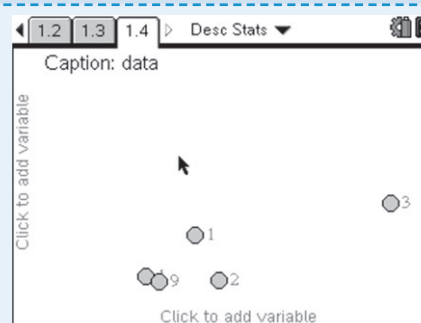
Draw a box and whisker diagram for this data:

Number	1	2	3	4	5
Frequency	3	4	6	5	2

Enter the data in lists called 'number' and 'freq' (see Example 45).

Add a new Data & Statistics page to your document.

Note: You do not need to worry about what this screen shows.



► Continued on next page

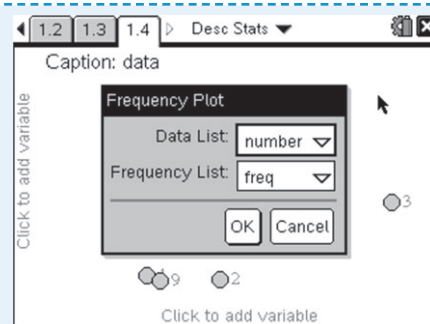
Press **menu** 2:Plot Properties | 5:Add X Variable with Frequency

Press **enter**

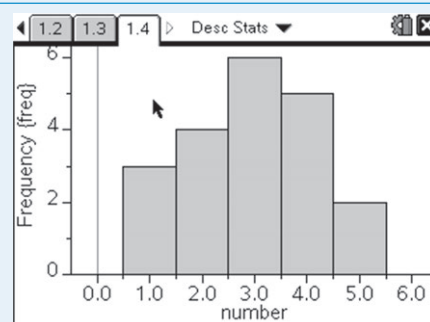
You will see this dialogue box.

From the drop-down menus, choose 'number' for the Data List and 'freq' for the Frequency List.

Press **enter**



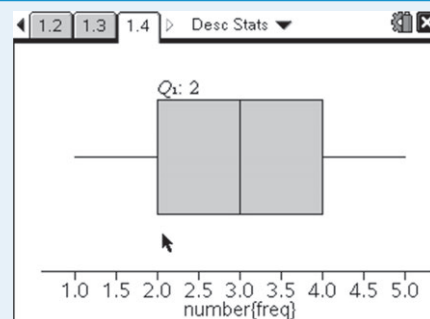
You should now see a frequency histogram.



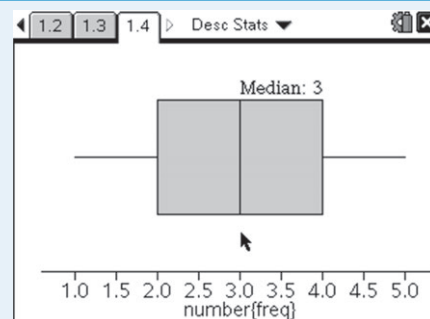
Press **menu** 1:Plot Type | 2:Box Plot

Press **enter**

You should now see a box plot (box and whisker diagram) for the data in the table.



Move the cursor over the plot and you will see the quartiles, Q_1 and Q_3 , the median, and the maximum and minimum values.



Calculating statistics

You can calculate statistics such as mean, median, etc. from a list, or from a frequency table.

5.7 Calculating statistics from a list

Example 50

Calculate the summary statistics for this data: 1, 1, 3, 9, 2

Enter the data in a list called 'data' (see Example 44).

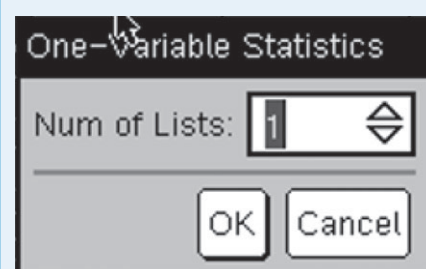
Add a new Calculator page to your document.

Press **menu** 6:Statistics | 1:Stat Calculations | 1:One-Var Statistics...

Press **enter**

This opens a dialogue box.

Leave the number of lists as 1 and press **enter**.



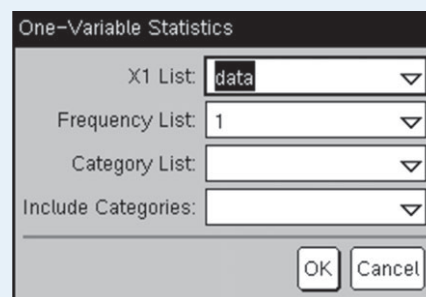
Mean, median, range, quartiles, standard deviation, etc. are called **summary statistics**.

▶ Continued on next page

This opens another dialogue box.

Choose 'data' from the drop-down menu for $X1$ List and leave the Frequency List as 1.

Press **enter**

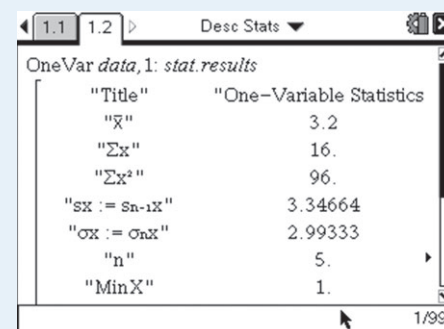


The information shown will not fit on a single screen.

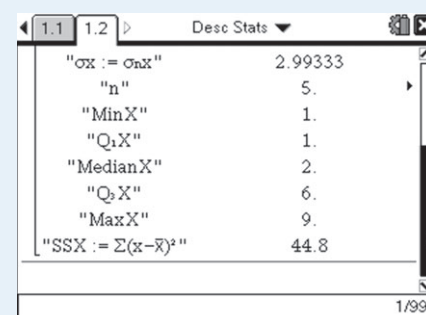
You can scroll up and down to see it all.

The statistics calculated for the data are:

mean	\bar{x}
sum	$\sum x$
sum of squares	$\sum x^2$
sample standard deviation	s_x
population standard deviation	σ_x



number	n
minimum value	$\text{Min}X$
lower quartile	Q_1X
median	$\text{Median}X$
upper quartile	Q_3X
maximum value	$\text{Max}X$
sum of squared deviations from the mean	SSX



Note: You should always use the population standard deviation (σ_x) in this course.

5.8 Calculating statistics from a frequency table

Example 51

Calculate the summary statistics for this data:

Number	1	2	3	4	5
Frequency	3	4	6	5	2

Enter the data in lists called 'number' and 'freq' (see Example 45).

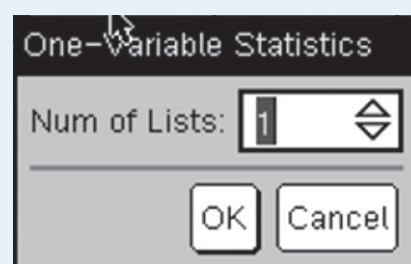
Add a new Calculator page to your document.

Press **menu** 6:Statistics | 1:Stat Calculations | 1:One-Var Statistics...

Press **enter**

This opens a dialogue box.

Leave the number of lists as 1 and press **enter**.

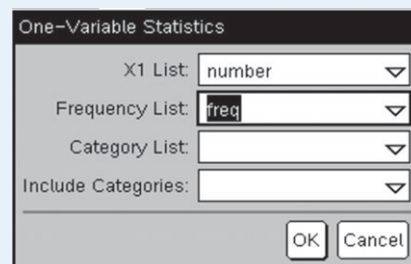


► Continued on next page

This opens another dialogue box.

From the drop-down menus, choose 'number' for X1 List and 'freq' for the Frequency List.

Press **enter**

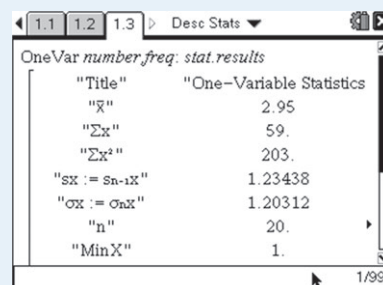


The information shown will not fit on a single screen.

You can scroll up and down to see it all.

The statistics calculated for the data are:

mean	\bar{x}
sum	$\sum x$
sum of squares	$\sum x^2$
sample standard deviation	s_x

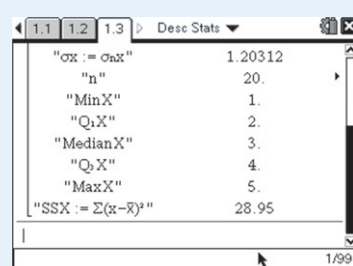
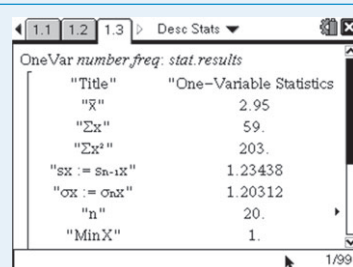


The information shown will not fit on a single screen.

You can scroll up and down to see it all.

The statistics calculated for the data are:

population standard deviation	σ_x
number	n
minimum value	MinX
lower quartile	Q_1X
median	MedianX
upper quartile	Q_3X
maximum value	MaxX
sum of squared deviations from the mean	SSX



Note: You should always use the population standard deviation (σ_x) in this course.

5.9 Calculating the interquartile range

Example 52

The interquartile range is the difference between the upper and lower quartiles ($Q_3 - Q_1$).

Calculate the interquartile range for this data:

Number	1	2	3	4	5
Frequency	3	4	6	5	2

First calculate the summary statistics for this data (see Example 51).

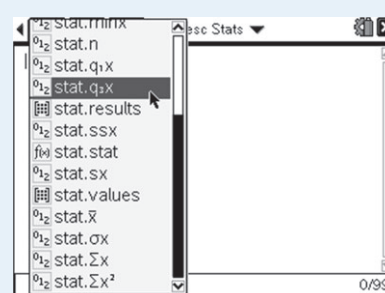
The values of the summary statistics are stored after One-Variable Statistics have been calculated and remain stored until the next time they are calculated.

Add a new Calculator page to your document.

Press **var**

A dialogue box will appear with the names of the statistical variables.

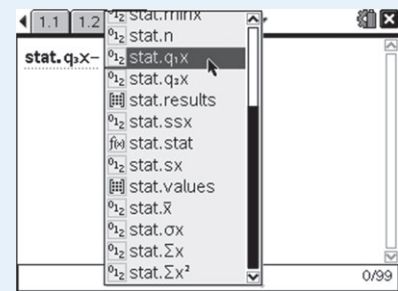
Scroll down to $\text{stat}.q_3x$ using the touchpad, or the $\blacktriangledown \blacktriangle$ keys, and then press **enter**.



Continued on next page

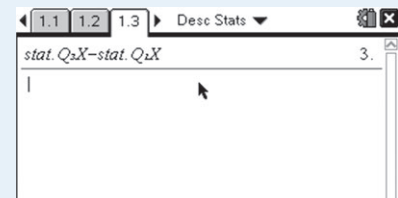
Type \ominus and press var again.

Scroll down to stat.q_1x using the touchpad, or the $\blacktriangledown \blacktriangle$ keys, and then press enter .



Press enter again.

The calculator now displays the result:
Interquartile range = $Q_3 - Q_1 = 3$



5.10 Using statistics

Example 53

Calculate $\bar{x} + \sigma_x$ for this data:

Number	1	2	3	4	5
Frequency	3	4	6	5	2

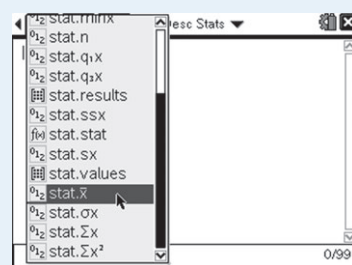
The calculator stores the values you calculate in One-Variable Statistics so that you can access them in other calculations. The values are stored until you do another One-Variable Statistics calculation.

First calculate the summary statistics for this data (see Example 51).
Add a new Calculator page to your document.

Press var

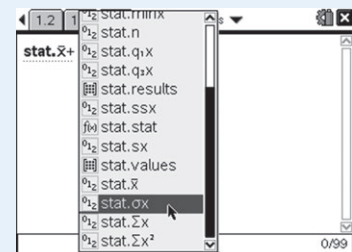
A dialogue box will appear with the names of the statistical variables.

Scroll down to $\text{stat.}\bar{x}$ using the touchpad, or the $\blacktriangledown \blacktriangle$ keys, and then press enter .



Type \oplus and press var again.

Scroll down to $\text{stat.}\sigma_x$ using the touchpad, or the $\blacktriangledown \blacktriangle$ keys, and then press enter .



Press enter again.

The calculator now displays the result:
 $\bar{x} + \sigma_x = 4.15$ (to 3 sf)



Calculating binomial probabilities

5.11 The use of nCr

Example 54

Find the value of $\binom{8}{3}$ (or ${}_8C_3$)

Open a new document and add a Calculator page.

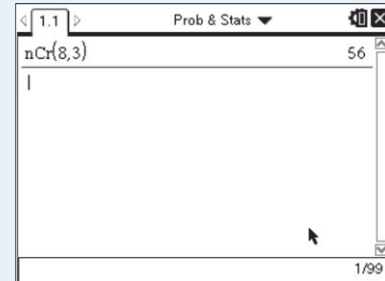
Press 5:Probability | 3:Combinations

Alternatively you can just type .

There is no need to worry about upper or lower case, the calculator recognises the key sequence and translates it accordingly.

Type 8,3

Press



Example 55

List the values of $\binom{4}{r}$ for $r = 0, 1, 2, 3, 4$

Open a new document and add a Calculator page.

Type 1

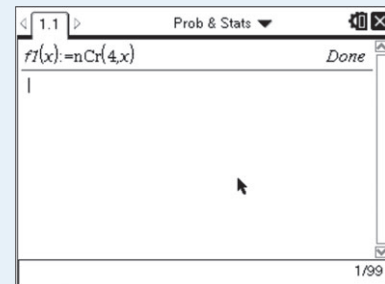
Press 5:Probability | 3:Combinations

Alternatively you can just type .

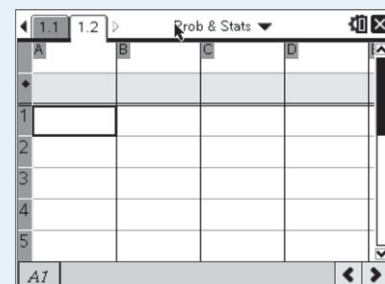
There is no need to worry about upper or lower case, the calculator recognises the key sequence and translates it accordingly.

Type 4, x

Press

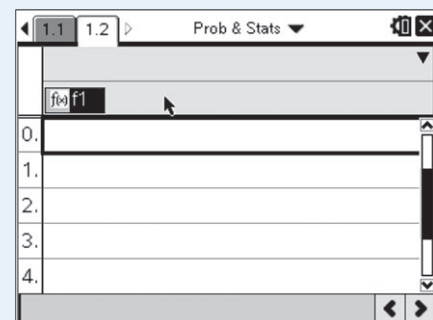


Press On and add a new Lists and Spreadsheet page to your document.



Press to switch from spreadsheet view to table view.

Press to display the function $f1(x)$



► Continued on next page

The table shows that

$$\binom{4}{0}=1, \binom{4}{1}=4, \binom{4}{2}=6, \binom{4}{3}=4 \text{ and } \binom{4}{4}=1$$

Prob & Stats	
x	f1(x):=
	nCr(4,x)
0.	1.
1.	4.
2.	6.
3.	4.
4.	1.

5.12 Calculating binomial probabilities

Example 56

X is a discrete random variable and $X \sim B(9, 0.75)$

Calculate $P(X = 5)$

$$P(x = 5) = \binom{9}{5} 0.75^5 0.25^4$$

The calculator can find this value directly

Open a new document and add a Calculator page.

Press **menu** 5:Probability | 3:Probability | 5:Distributions | D:Binomial Pdf...

Enter the number of trials, probability of success and the X value. Click on OK

Binomial Pdf	
Num Trials, n:	9
Prob Success, p:	0.75
X Value:	5
<input type="button" value="OK"/> <input type="button" value="Cancel"/>	

The calculator shows that

$$P(X = 5) = 0.117 \text{ (to 3 sf)}$$

You can also type the function straight in without using the dialogue box.

Prob & Stats	
binomPdf(9,0.75,5)	
0.116798	
1/99	

Example 57

X is a discrete random variable and $X \sim B(7, 0.3)$

Calculate the probabilities that X takes the values $\{0, 1, 2, 3, 4, 5, 6, 7\}$

Open a new document and add a Calculator page.

Press **menu** 5:Probability | 3:Probability | 5:Distributions | D:Binomial Pdf...

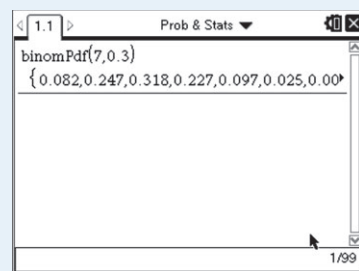
Enter the number of trials, probability of success and leave the X value blank.

Click on OK

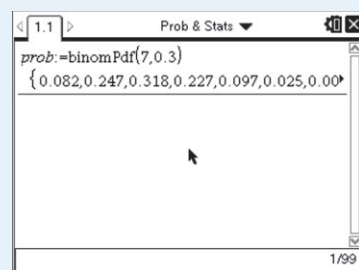
Binomial Pdf	
Num Trials, n:	7
Prob Success, p:	0.3
X Value:	(optional)
<input type="button" value="OK"/> <input type="button" value="Cancel"/>	

► Continued on next page

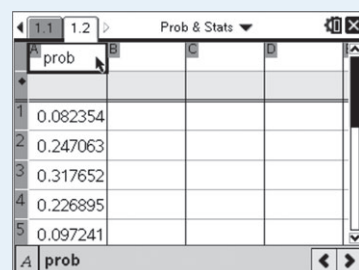
The calculator displays each of the probabilities.
To see the remaining values scroll the screen to the right.
The list can also be transferred to a Lists & Spreadsheet page.



To store the list in a variable named “prob” type:
`prob:=binomPdf(7,0.3)`
or use the dialogue box as you did before.
Use **ctrl** **:=** to enter :=



Press **On** and add a new Lists & Spreadsheet page
At the top of the first column type prob
Press **enter**
The binomial probabilities are now displayed in the first column.



Example 58

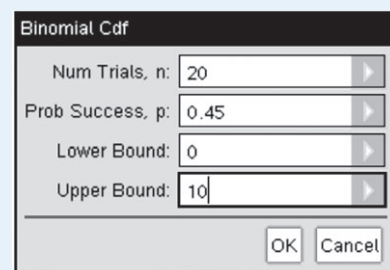
X is a discrete random variable and $X \sim B(20, 0.45)$

Calculate

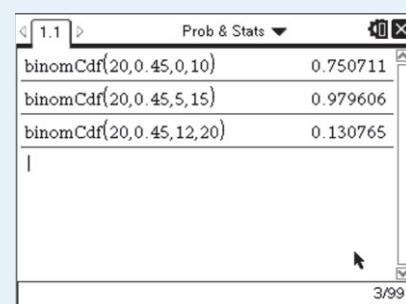
- the probability that X is less than or equal to 10
- the probability that X lies between 5 and 15 inclusive
- the probability that X is greater than 11

Open a new document and add a Calculator page.
Press **menu** 5:Probability | 3:Probability | 5:Distributions |
E:Binomial Cdf

Enter the number of trials and the probability of success
The lower bound in this case is 0 and the upper bound
is 10.
Click on OK



- $P(X \leq 10) = 0.751$ (to 3 sf)
 - $P(5 \leq X \leq 15) = 0.980$ (to 3 sf)
 - $P(X > 11) = 0.131$ (to 3 sf)
- Note: the lower bound is 12 here.



Calculating Poisson probabilities

5.13 Calculating Poisson probabilities

Example 59

X is a discrete random variable and $X \sim Po(0.5)$

Calculate i $P(X = 2)$

ii $P(X \leq 2)$

iii $P(X > 2)$

i $P(X = 2) = \frac{e^{-0.5} \times (0.5)^2}{2!}$

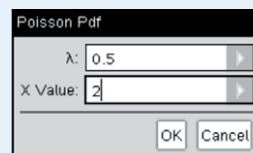
The calculator can find this value directly.

Open a new document and add a Calculator page.

Press  5:Probability | 5:Distributions | H:Poisson Pdf...

Enter the parameter and the X value.

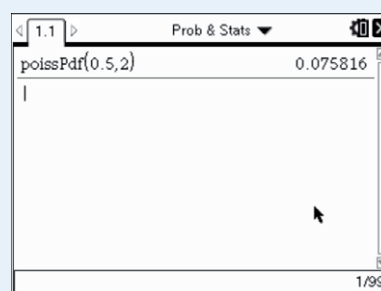
Click on OK



The calculator shows that

$P(X = 2) = 0.0758$ (to 3 sf)

You can also type the function straight in without using the dialogue box.



ii $P(X \leq 2) = \frac{e^{-0.5} \times (0.5)^0}{0!} + \frac{e^{-0.5} \times (0.5)^1}{1!} + \frac{e^{-0.5} \times (0.5)^2}{2!}$

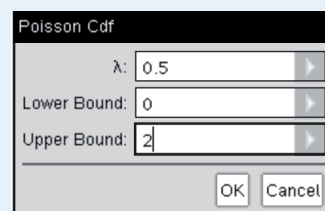
The calculator can find this value directly.

Open a new document and add a Calculator page.

Press  5:Probability | 5:Distributions | I:Poisson Cdf...

Enter the parameter, the lower bound 0 and the upper bound 2.

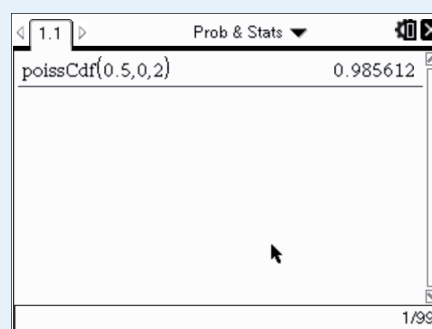
Click on OK



The calculator shows that

$P(X \leq 2) = 0.986$ (to 3 sf)

You can also type the function straight in without using the dialogue box.



▶ Continued on next page

$$\text{iii } P(X > 2) = \frac{e^{-0.5} \times (0.5)^3}{3!} + \frac{e^{-0.5} \times (0.5)^4}{4!} + \frac{e^{-0.5} \times (0.5)^5}{5!}$$

$$= 1 - P(X \leq 2)$$

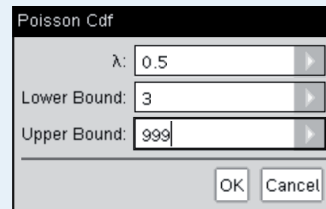
The calculator can find this value directly.

Open a new document and add a Calculator page.

Press  5:Probability | 5:Distributions | I:Poisson Cdf...

Enter the parameter, the lower bound 3 and the upper bound 999. (999 is a very large number in this distribution)

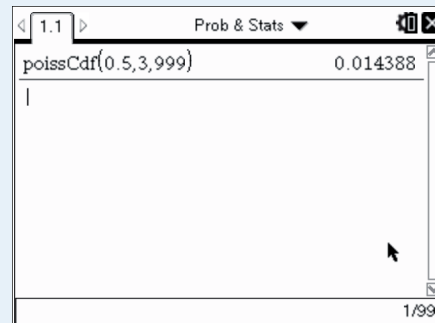
Click on OK



The calculator shows that

$$P(X > 2) = 0.0144 \text{ (to 3 sf)}$$

You can also type the function straight in without using the dialogue box – or you could also calculate $P(X > 2)$ from $P(X \leq 2)$.





Example 60

If $X \sim \text{Po}(\lambda)$ find the value of λ , correct to 3 decimal places, given that $P(X = 2) = 0.035$

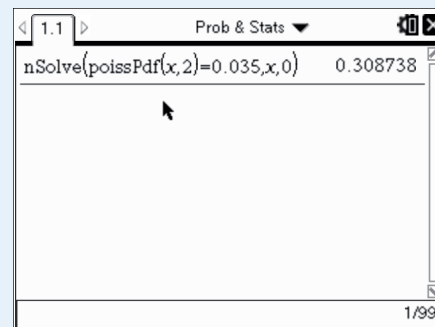
There is no inverse Poisson function on the TI-Nspire, so instead you should use the numerical solver function to find a value of λ when you are given a probability.

Open a new document and add a Calculator page.

Press  3:Algebra | 1:Numerical Solve

Press  5:Probability | 5:Distributions | H:Poisson Pdf... or type PoissonPdf(and enter the value of λ as x , the value of n as 2 and the probability as 0.035. It is necessary to enter the variable x in the numerical solver and also an initial guess – 0 is close enough.

The required value of λ is 0.309 (to 3 sf).



Calculating normal probabilities

5.14 Calculating normal probabilities from X-values

Example 61

A random variable X is normally distributed with a mean of 195 and a standard deviation of 20, or $X \sim N(195, 20^2)$. Calculate

- the probability that X is less than 190
- the probability that X is greater than 194
- the probability that X lies between 187 and 196.

Open a new document and add a Calculator page.

Press **menu** 5:Probability | 5:Distributions | 2:Normal Cdf

Press **enter**

You need to enter the values Lower Bound, Upper Bound, μ and σ in the dialogue box.

For the Lower Bound, enter -9×10^{999} as $-9\text{E}999$. This is the smallest number that can be entered in the GDC, so it is used in place of $-\infty$.

To enter the E , you need to press the key marked **EE**.

- $P(X < 190)$

Leave the Lower Bound as $-9\text{E}999$.

Change the Upper Bound to 190.

Change μ to 195 and σ to 20.

$P(X < 190) = 0.401$ (to 3 sf)

- $P(X > 194)$

Change the Lower Bound to 194.

For the Upper Bound, enter 9×10^{999} as $9\text{E}999$. This is the largest number that can be entered in the GDC, so it is used instead of $+\infty$. Leave μ as 195 and σ as 20.

$P(X > 194) = 0.520$ (to 3 sf)

- $P(187 < X < 196)$

Change the Lower Bound to 187 and the Upper Bound to 196; leave μ as 195 and σ as 20.

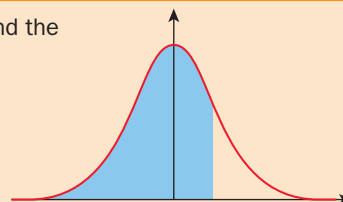
$P(187 < X < 196) = 0.175$ (to 3 sf)

normCdf(-9.E999,190,195,20)	0.401294
normCdf(194,9.E999,195,20)	0.519939
normCdf(187,196,195,20)	0.175361

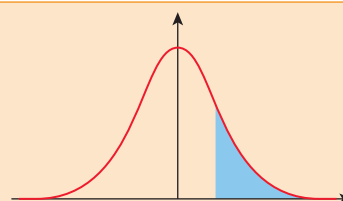
It can be quicker to type the function directly into the calculator, without using the menus and the wizard, but there are a lot of parameters to remember for the function normCdf.

5.15 Calculating X-values from normal probabilities

When using the inverse normal function (invNorm), make sure that you find the probability on the correct side of the normal curve. The areas are always the lower tail, that is, they are of the form $P(X < x)$.



If you are given the upper tail, $P(X > x)$, you must first subtract the probability from 1 to before you can use invNorm.



Example 62

A random variable X is normally distributed with a mean of 75 and a standard deviation of 12, or $X \sim N(75, 12^2)$.

If $P(X < x) = 0.4$, find the value of x .

You are given a *lower-tail* probability, so you can find $P(X < x)$ directly.

Open a new document and add a Calculator page.

Press **menu** 5:Probability | 5:Distributions | 3:Inverse Normal...

Press **enter**

Enter the probability (area = 0.4), mean ($\mu = 75$) and standard deviation ($\sigma = 12$) in the dialogue box.

It can be quicker to type the function directly into the calculator, without using the menus and the wizard, but there are a lot of parameters to remember for the function `invNorm`.

So, if $P(X < x) = 0.4$ then $x = 72.0$ (to 3 sf).

Example 63

A random variable X is normally distributed with a mean of 75 and a standard deviation of 12, or $X \sim N(75, 12^2)$.

If $P(X > x) = 0.2$, find the value of x .

You are given an *upper-tail* probability, so you must first find $P(X < x) = 1 - 0.2 = 0.8$. You can now use the `invNorm` function as before.

Open a new document and add a Calculator page.

Press **menu** 5:Probability | 5:Distributions | 3:Inverse Normal...

Press **enter**

Enter the probability (area = 0.8), mean ($\mu = 75$) and standard deviation ($\sigma = 12$) in the dialogue box.

So, if $P(X > x) = 0.2$ then $x = 85.1$ (to 3 sf).

This sketch of a normal distribution curve shows the value of x and the probabilities for Example 63.

