

Prove by contradiction that, if  $n^2$  is even, then  $n$  is even

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Assume that  $n$  is odd  $n = 2k + 1$

$$n^2 = (2k + 1)^2$$

$$n^2 = 4k^2 + 4k + 1$$

$$n^2 = 2(2k^2 + 2k) + 1$$

This is an odd number

This is a **contradiction**, since  $n^2$  is an even number

Therefore if  $n^2$  is even, then  $n$  is even