\$10 000 is invested in a bank receiving 4% interest at the end of each year. How long does it take before the investment doubles in value?

> After 1 year A =  $10\ 000 \times 1.04$ After 2 years A =  $(10\ 000 \times 1.04) \times 1.04$ A =  $10\ 000 \times 1.04^2$ After 3 years A =  $10\ 000 \times 1.04^3$

After **n** years  $A = 10000 \times 1.04^{n}$ 

How long does it take before the investment doubles in value?

 $10\ 000 \times 1.04^n = 20\ 000$ 

Solve for n

$$1.04^n = \frac{20\ 000}{10\ 000}$$
$$1.04^n = 2$$

Take logs of both sides

$$\ln(1.04^{n}) = \ln(2)$$
  
nln(1.04) = ln(2)  
n =  $\frac{\ln(2)}{\ln(1.04)}$ 



We can also use the calculator to solve. The table function is useful here

 $10\ 000 \times 1.04^n = 20\ 000$ 



n = 18

You can also solve using the graph mode



n = 18