The gradient of $y = x^2 + ax + b$ at the point (1,-3) is -4. Find \bf{a} and \bf{b} .

$$y = x^2 + ax + b$$

Find the gradient function

$$\frac{dy}{dx} = 2x + a$$

gradient =-4 when x = 1 substitute $\frac{dy}{dx} = -4$, x = 1

$$-4 = 2(1) + a$$

simplify

$$-4 = 2 + a$$
$$-6 = a$$

$$y = x^2 + ax + b$$

(1,-3) is a point on the curve. substitute x = 1, y=-3

$$-3 = 1^2 + a(1) + b$$

simplify

$$-4 = a + b$$

we know a = -6

$$-4 = -6 + b$$
$$2 = b$$

$$a = -6$$

$$b = 2$$

