

Consider the function  $f(x) = x^3 - 4x^2 - x + 6$ ,  $x \in \mathbb{R}$

The graph of  $f$  is translated two units to the left and 3 units up to form the function  $g(x)$ . Express  $g(x)$  in the form  $ax^3 + bx^2 + cx + d$  where  $a, b, c, d \in \mathbb{Z}$

---

$$f(x) = x^3 - 4x^2 - x + 6$$

$f$  is translated **two units to the left**

and **3 units up** to form  $g(x)$

$$g(x) = f(x + 2) + 3$$

$$g(x) = (x + 2)^3 - 4(x + 2)^2 - (x + 2) + 6 + 3$$

$$g(x) = x^3 + 6x^2 + 12x + 8 - 4x^2 - 16x - 16 - x - 2 + 9$$

$$g(x) = x^3 + 2x^2 - 5x - 1$$