Two boxes each contain three cards.
The first box contains cards labelled 1,3 and 5
The second box contains cards labelled 2, 4 and 6.
In a game, a player draws one card at random from each box and his score, $X$, is the sum of the numbers on the two cards.
Complete the following probability distribution

| $x$ | 3 | 5 |  |  | 11 |
| ---: | :---: | :---: | :---: | :---: | :---: |
| $P(X=x)$ | $\frac{1}{9}$ |  |  |  | $\frac{2}{9}$ |

Calculate $E(X)$
a) There are 9 possible outcomes

|  | 1 | 3 | 5 |
| :---: | :---: | :---: | :---: |
| 2 | 3 | 5 | 7 |
| 4 | 5 | 7 | 9 |
| 6 | 7 | 9 | 11 |

Here's the probability distribution for $\boldsymbol{X}$

| $x$ | 3 | 5 | 7 | 9 | 11 |
| ---: | :---: | :---: | :---: | :---: | :---: |
| $P(X=x)$ | $\frac{1}{9}$ | $\frac{2}{9}$ | $\frac{3}{9}$ | $\frac{2}{9}$ | $\frac{1}{9}$ |

b)

$$
\begin{aligned}
& \mathrm{E}(X)=\mu=\sum_{x} x \mathrm{P}(X=x) \\
& E(X)=3 \times \frac{1}{9}+5 \times \frac{2}{9}+7 \times \frac{3}{9}+9 \times \frac{1}{9}+11 \times \frac{1}{9} \\
& E(X)=\frac{3}{9}+\frac{10}{9}+\frac{21}{9}+\frac{9}{9}+\frac{11}{9} \\
& E(X)=\frac{54}{9} \\
& E(X)=6
\end{aligned}
$$

