## (11) (S1) 囲

The amount of caffeine, $\boldsymbol{X}$ in mg, found in a cup of tea can be modelled by the normal distribution $X \sim N(26,5)$
a) Find the probability that a randomly selected cup of tea contains at least 27 mg of caffeine.
b) 10 cups of tea are randomly selected. Find the probability that more than 5 of these cups has at least 24 mg of caffeine.


| a) <br> Lower $=27$ <br> Upper $=9 \times 10^{99}$ <br> Standard deviation $=\sqrt{\mathbf{5}}$ <br> Mean $=26$ $P(X>27) \approx 0.327$ <br> \{a higher degree of accuracy of this value will be used in the next part of the question\} |  |
| :---: | :---: |
| b) This question becomes one about the Binomial Distribution. $\begin{aligned} & \mathrm{n}=10 \\ & \mathrm{p}=0.32736 \end{aligned}$ <br> Let $Y$ be number of cups of tea that have at least 27 mg of caffeine. $\begin{aligned} & Y \sim B(10,0.32736) \\ & P(Y \geq 6) \approx 0.0706 \\ & \hline \end{aligned}$ |  |

