

Systems of Equations - Unique Solution

$$x + y + 2z = 0 \quad \textcircled{1}$$

$$2x - y + z = -6 \quad \textcircled{2}$$

$$3x + 4y - z = -6 \quad \textcircled{3}$$

$$\textcircled{2} + \textcircled{3} \quad 5x + 3y = -12 \quad \textcircled{A}$$

$$2x \textcircled{3} \quad 6x + 8y - 2z = -12$$

$$\textcircled{1} \quad x + y + 2z = 0$$

$$7x + 9y = -12 \quad \textcircled{B}$$

$$3x \textcircled{A} \quad 15x + 9y = -36 \quad \textcircled{C}$$

$$\textcircled{C} - \textcircled{B} \quad 8x = -24$$

$$x = -3$$

$$\begin{aligned} \text{sub in } \textcircled{B} \quad -21 + 9y &= -12 \\ 9y &= 9 \\ y &= 1 \end{aligned}$$

$$\begin{aligned} \text{sub in } \textcircled{1} \quad -3 + 1 + 2z &= 0 \\ -2 + 2z &= 0 \\ 2z &= 2 \\ z &= 1 \end{aligned}$$

Unique solution at $(-3, 1, 1)$

